

May 15th, 2024

Growth estimates for p-harmonic Green functions on weighted \mathbb{R}^n and metric spaces

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As shown by Serrin in 1964, the growth at an isolated singularity of solutions to the elliptic equation div $A(x, \nabla u) = 0$ in \mathbb{R}^n (including p-harmonic functions with p > 1) is exactly determined by the dimension n and the parameter p associated with the equation. In this talk, I will discuss growth and integrability properties for p-harmonic Green functions and their gradients on weighted \mathbb{R}^n , with a p-admissible weight, as well as on complete metric spaces equipped with a doubling measure supporting a p-Poincaré inequality. In these situations, the dimension n is replaced by the local growth of the underlying measure near the isolated singularity, and the obtained growth and integrability exponents are sharp.