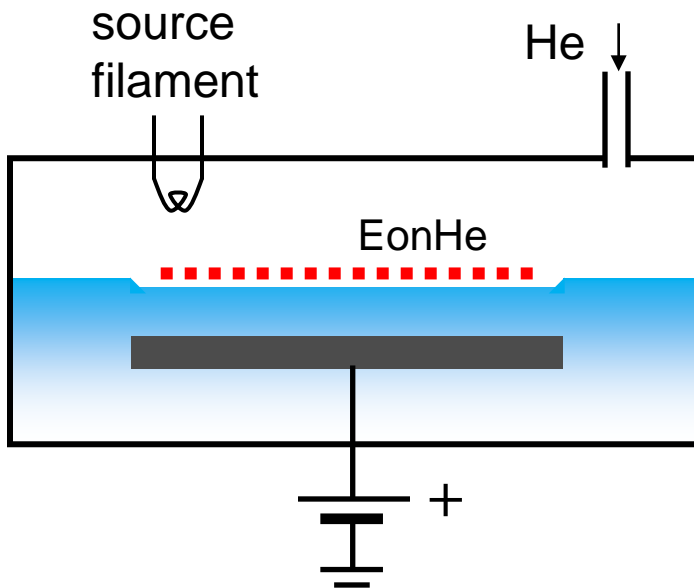
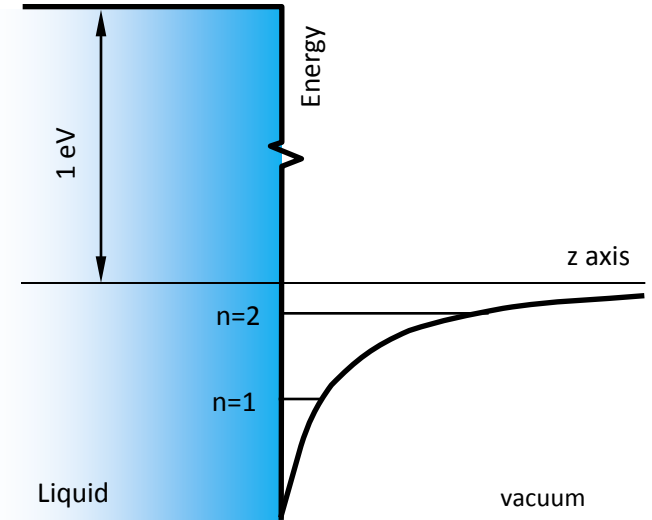
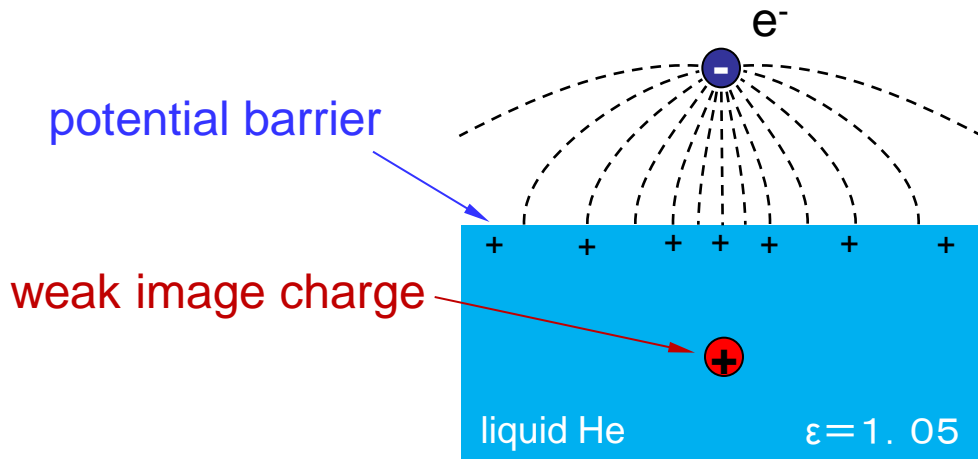


Electrons on helium under CR excitation



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Quantum Dynamics Unit, OIST Graduate University



Transverse confinement

Image potential + surface barrier

Lateral confinement

Electrostatic potential due to positively biased gate

$$\Gamma_p = \frac{V_C}{E_{th}} = \frac{e^2 \sqrt{\pi n_s}}{4\pi\epsilon\epsilon_0 k_B T}$$

Thermal fluctuations

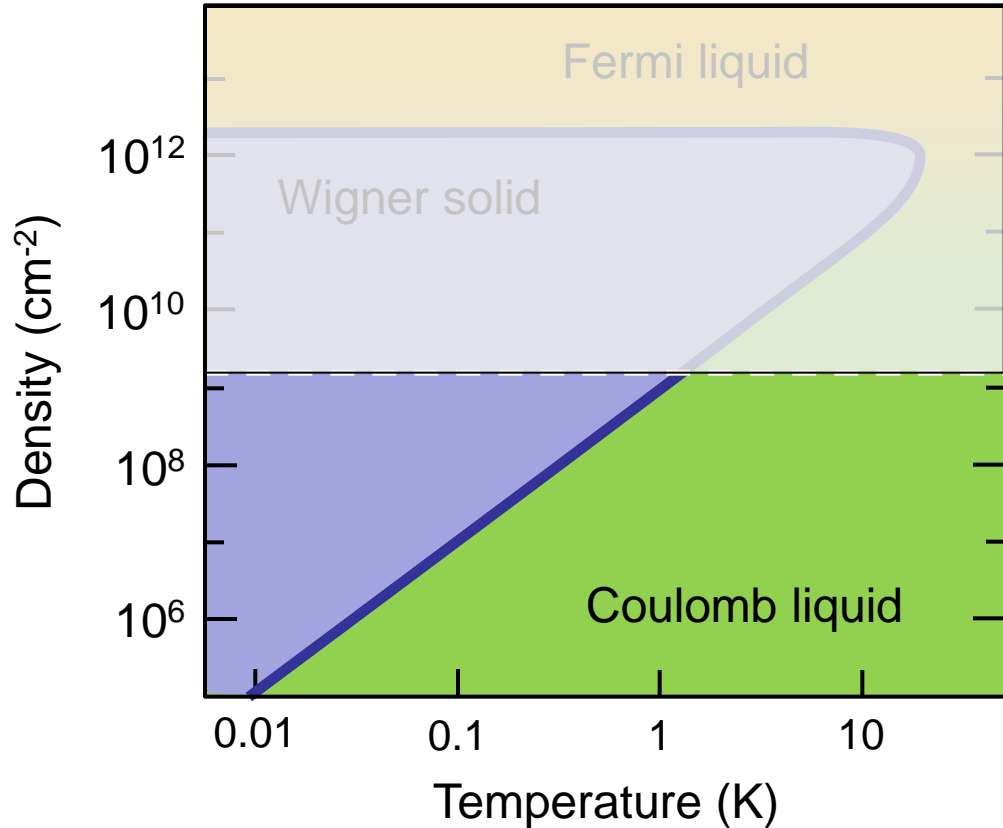
$$\epsilon = 1$$

$$r_p = \frac{E_f}{V_C} = \frac{4\pi\epsilon\epsilon_0 \hbar^2 \pi n_s}{e^2 \sqrt{\pi n_s} m^*}$$

Quantum fluctuations

$$m^* = m_e$$

$$n_s < 2 \times 10^9 \text{ cm}^{-2}$$

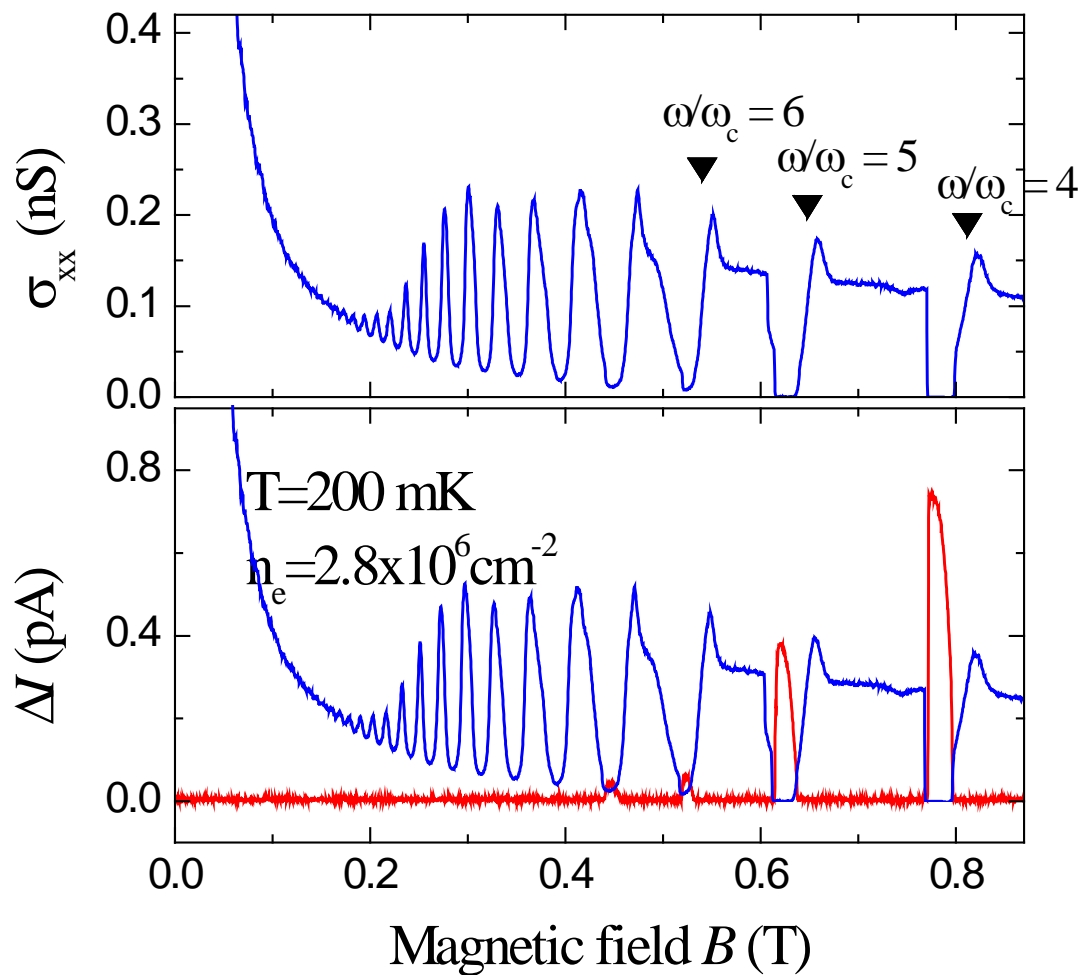
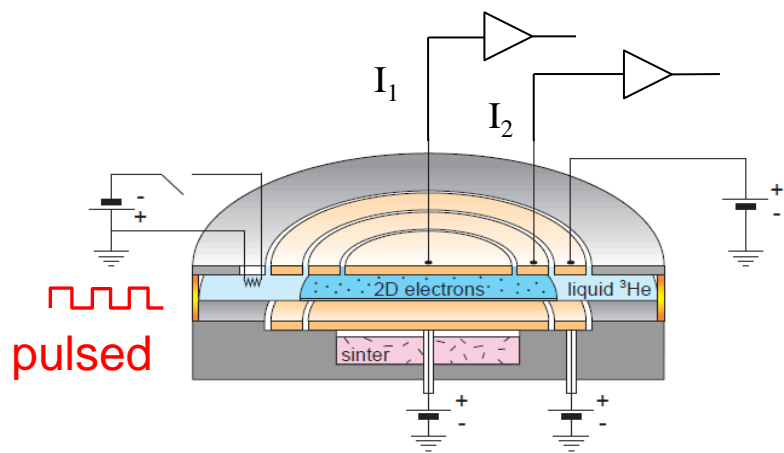
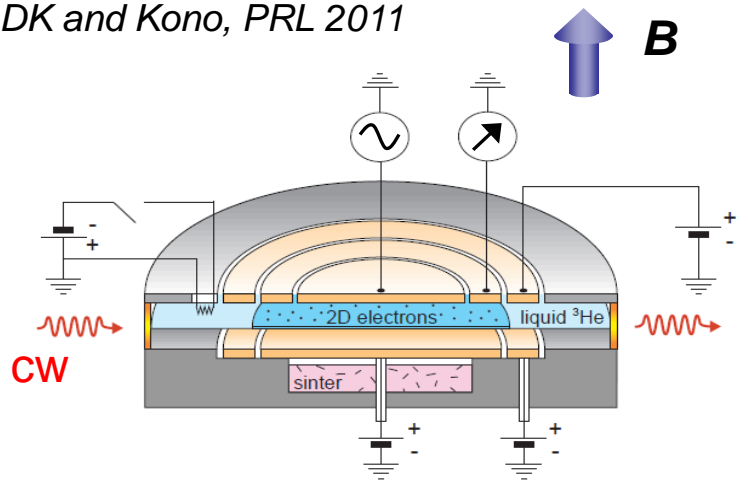


2DEG in
semiconductors

$$\epsilon \approx 10, m^* \approx 0.1 m_e$$

$$n_s > 5 \times 10^{10} \text{ cm}^{-2}$$


DK and Kono, PRL 2011



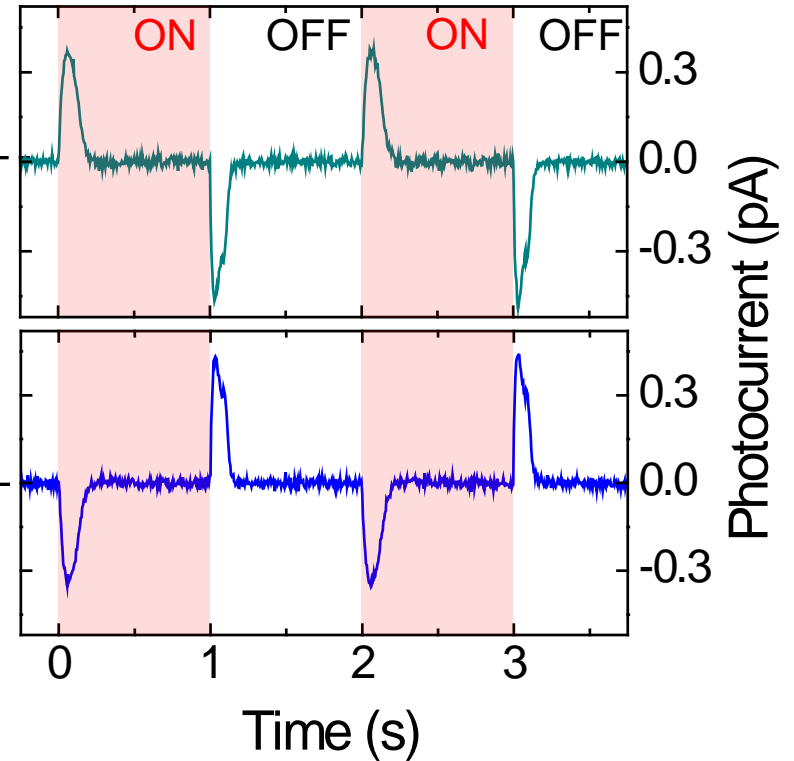
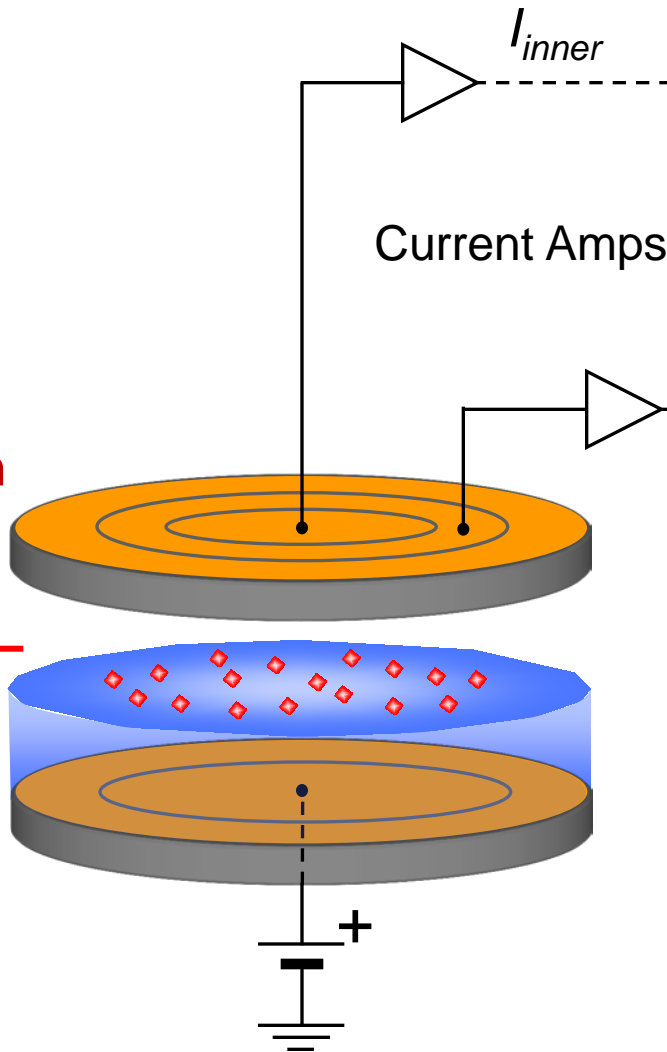
DK, Chepelianskii, Kono, *J. Phys. Soc. Jpn.* 2012

Fix B -field
at minima
of σ_{xx}

Microwave
modulation
ON/OFF



MW



When MW switched ON
Positive image charge released
Electrons move away from the center

Momentum balance equation

Yu. P. Monarkha

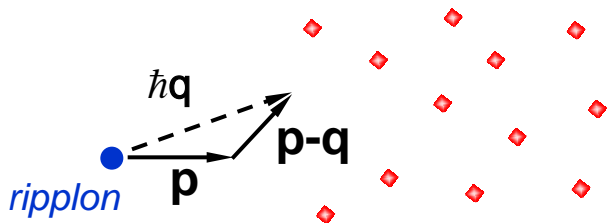


$$\mathbf{F}_{friction} = -N_e m v_{eff} \mathbf{u}_d$$

$$\sigma_{xx} = \frac{e^2 n_s}{m_e} \frac{v_{eff}}{\omega_c^2 + v_{eff}^2}$$

$$\mathbf{F}_{friction} = -\sum_{\mathbf{q}} \hbar \mathbf{q} \cdot P_{\mathbf{p}, \mathbf{p}-\mathbf{q}} = -\frac{N_e}{\hbar^2 S} \sum \hbar \mathbf{q} \cdot U(\mathbf{q}) \cdot \underbrace{\xi(\mathbf{q}, \omega - \mathbf{q} \cdot \mathbf{u}_d)}$$

Doppler shift in laboratory frame



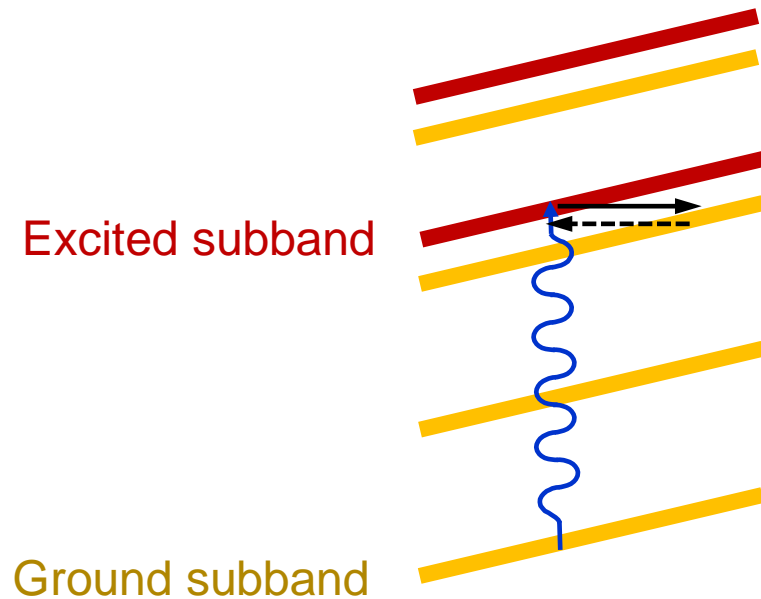
$\xi(\mathbf{q}, \omega)$ - Dynamical Structure Factor (DSF)

$$\mathbf{F}_{friction} = -\frac{N_e}{\hbar^2 S} \sum_{\mathbf{q}} \hbar \mathbf{q} \sum_{n, n'} \rho_n U_{n, n'}(\mathbf{q}) \left[\underbrace{N_q + 1}_{\text{creation of ripplon}} S_{n, n'}(\mathbf{q}, \omega_{n, n'} - \mathbf{q} \cdot \mathbf{u}_d) - \underbrace{N_q}_{\text{annihilation of ripplon}} S_{n, n'}(\mathbf{q}, \omega_{n, n'} + \mathbf{q} \cdot \mathbf{u}_d) \right]$$

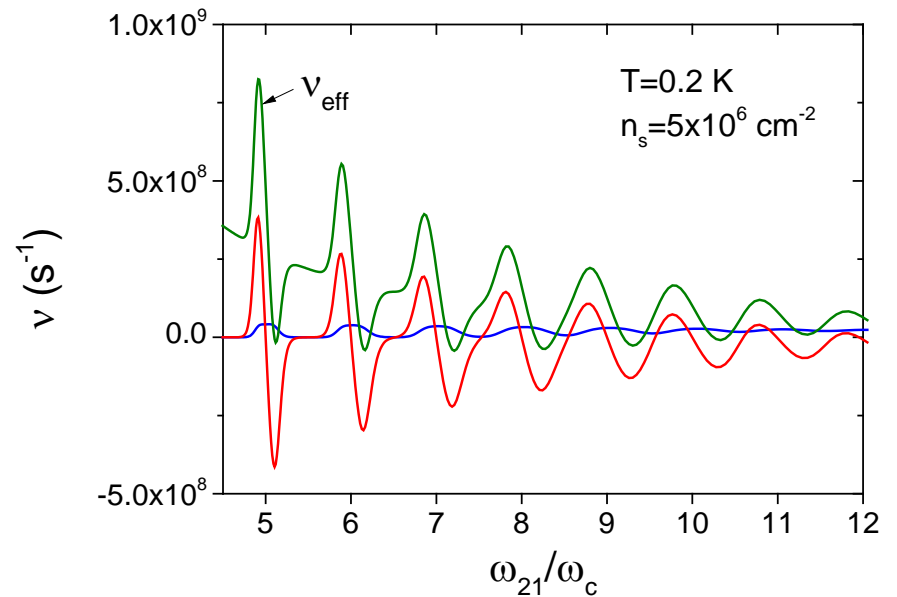
$$\mathbf{F}_{friction} \sim -\sum_{\mathbf{q}} \hbar \mathbf{q} \sum_{n, n'} \chi_{n, n'}(\mathbf{q}) \cdot S_{n, n'}(\mathbf{q}, \omega_{n, n'} + \mathbf{q} \cdot \mathbf{u}_d) \cdot (\rho_n - \rho_{n'}) e^{\frac{\hbar \omega_{n, n'}}{k_B T_e}} e^{-\frac{\hbar \mathbf{q} \cdot \mathbf{u}_d}{k_B T_e}}$$

$$\begin{aligned}
 v_{\text{inter}} \sim & \sum_{\mathbf{q}} \hbar \mathbf{q} \sum_{n>n'} \chi_{n,n'}(\mathbf{q}) \cdot \underbrace{S_{n,n'}(q, \omega_{n,n'})}_{\text{DSF}} \cdot (\rho_n + \rho_{n'} e^{\frac{\hbar \omega_{n,n'}}{k_B T_e}}) + \\
 & + \frac{\hbar}{k_B T} \sum_{\mathbf{q}} \hbar \mathbf{q} \sum_{n>n'} \chi_{n,n'}(\mathbf{q}) \cdot \underbrace{S'_{n,n'}(q, \omega_{n,n'})}_{\text{derivative of DSF}} \cdot (\rho_n - \rho_{n'} e^{\frac{\hbar \omega_{n,n'}}{k_B T_e}})
 \end{aligned}$$

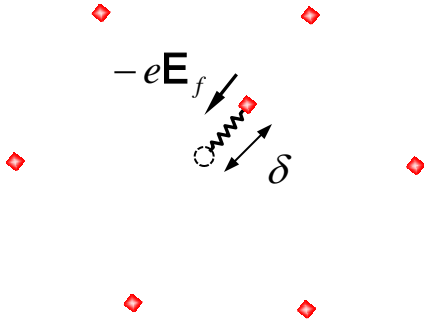
Tilted LLs in dc E-field



non-zero for nonequilibrium population



Dykman, Khazan 1979

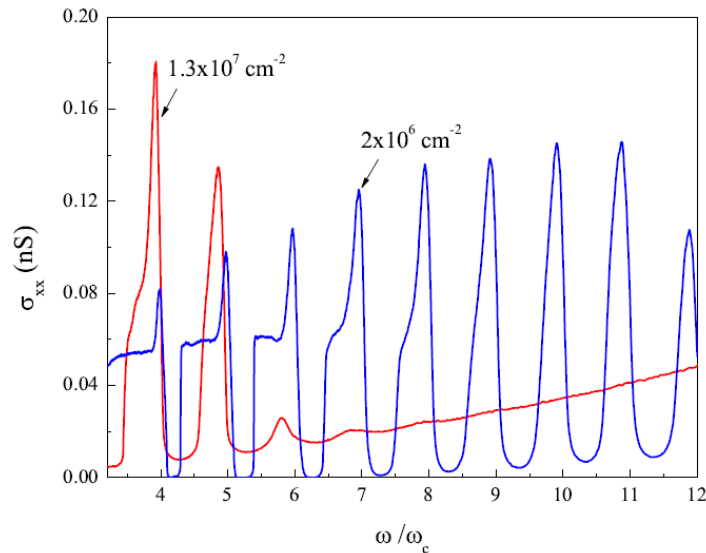


$$\frac{k\delta^2}{2} \approx k_B T_e \Rightarrow \langle E_f \rangle \approx n_s^{3/4} \sqrt{4\pi k_B T_e}$$

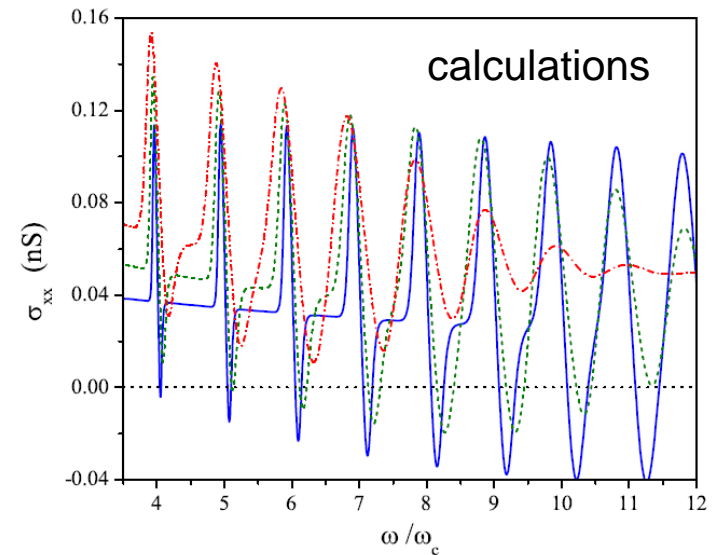
$$\mathbf{u}_d \rightarrow \mathbf{u}_f$$

$$S^{(me)}(q, \omega) = \langle S(q, \omega - \mathbf{q} \cdot \mathbf{u}_f) \rangle$$

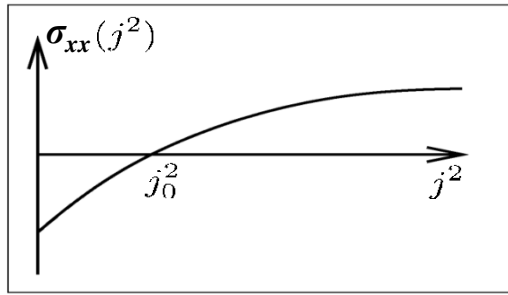
DK, Monarkha, Kono, PRL 2013



Coulomb broadening of DSF



There exists (some) mechanism
 leading to **absolute negative** σ_{xx}



$$\frac{\partial \rho_s}{\partial t} = -\nabla \vec{j} = \sigma \nabla_r^2 V$$

$$\nabla^2 V = -\rho_s \delta(z)$$

$$\rho_k \sim \exp\left(-\frac{\sigma k}{2} t\right) \rightarrow \infty$$

Instability and formation of current domains

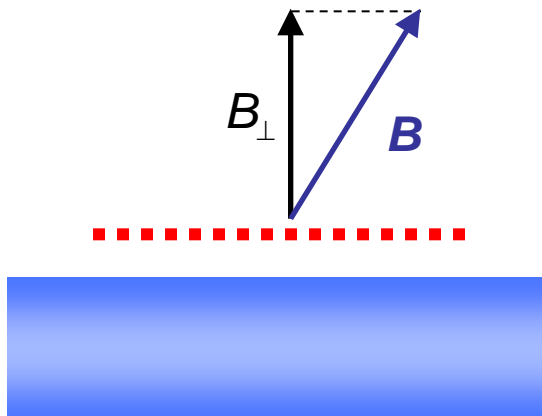
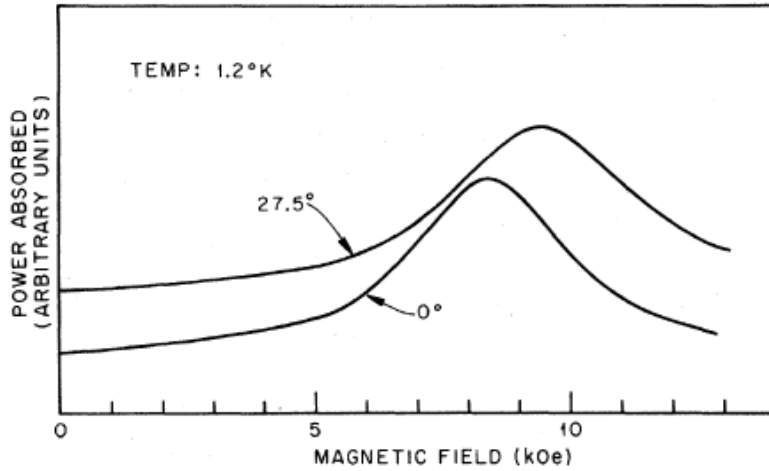
Andreev, Aleiner, Millis, PRL 2003

Other explanations are proposed, e.g. Entin and Magarill: [arXiv: 1504.03422](https://arxiv.org/abs/1504.03422)

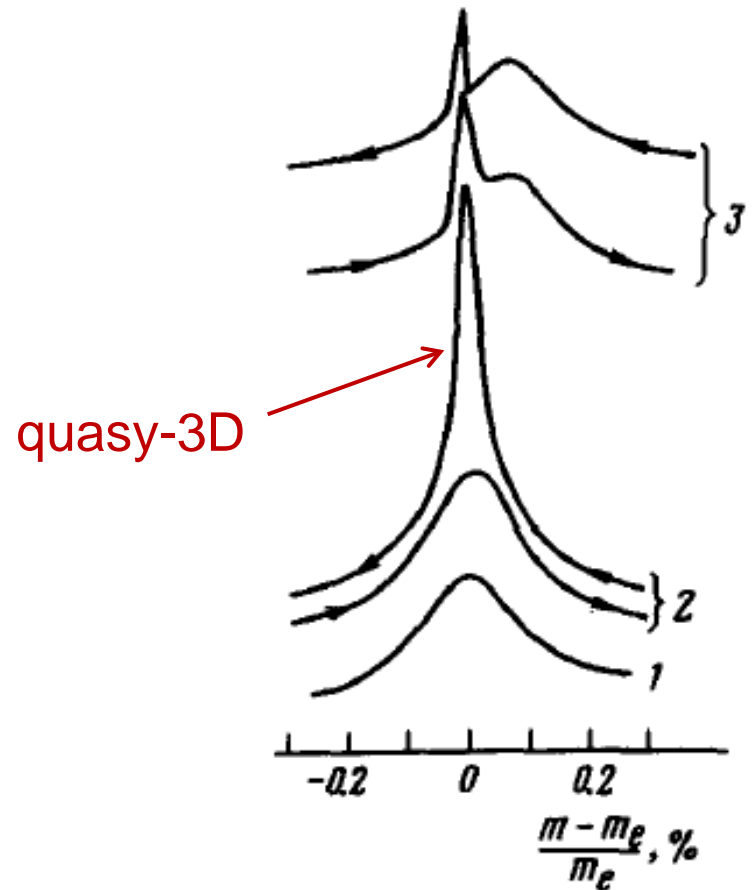
ZRS in electrons on helium have interesting properties

- self-organized oscillations (previous talk)
- incompressibility (next talk)

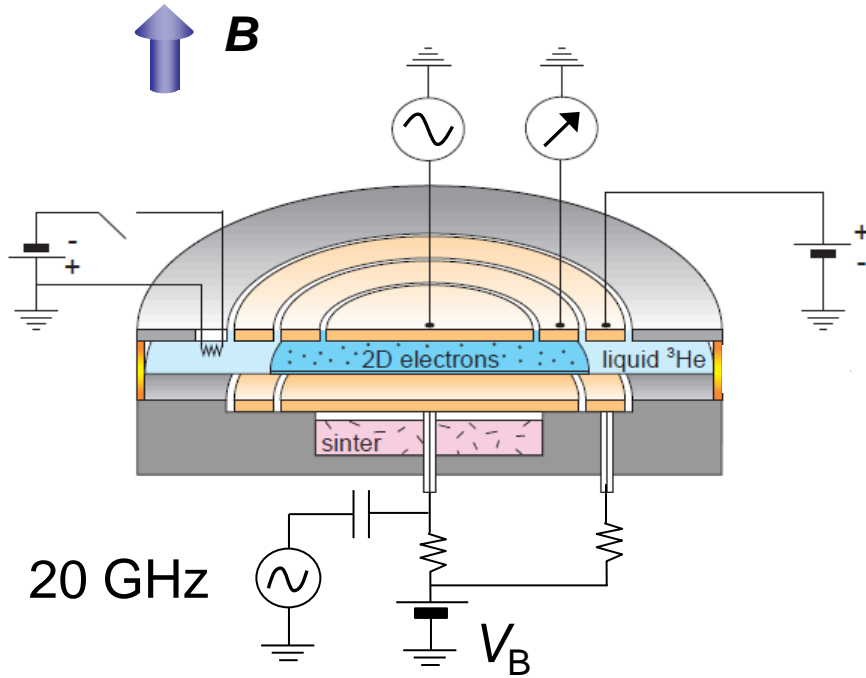
Brown, Grimes 1972



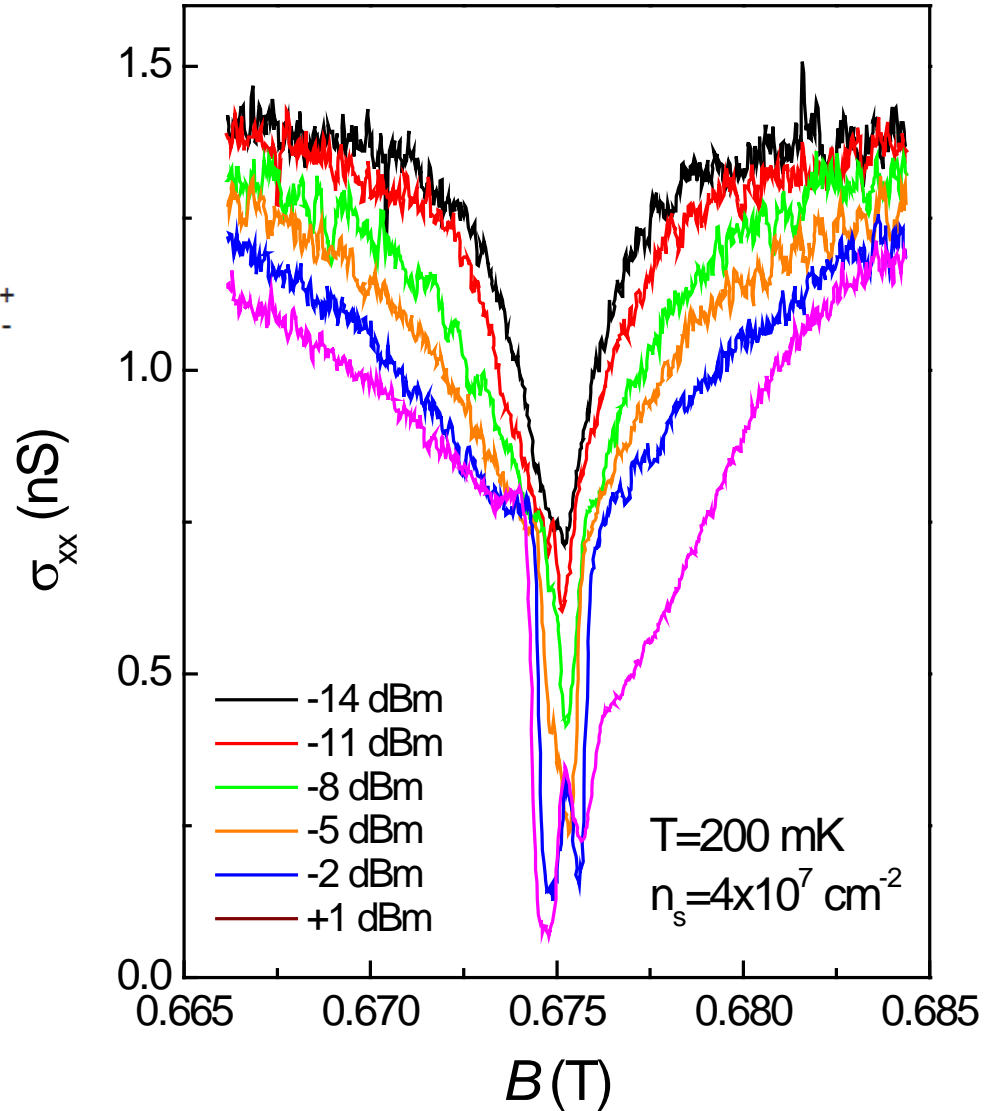
Edelman 1972



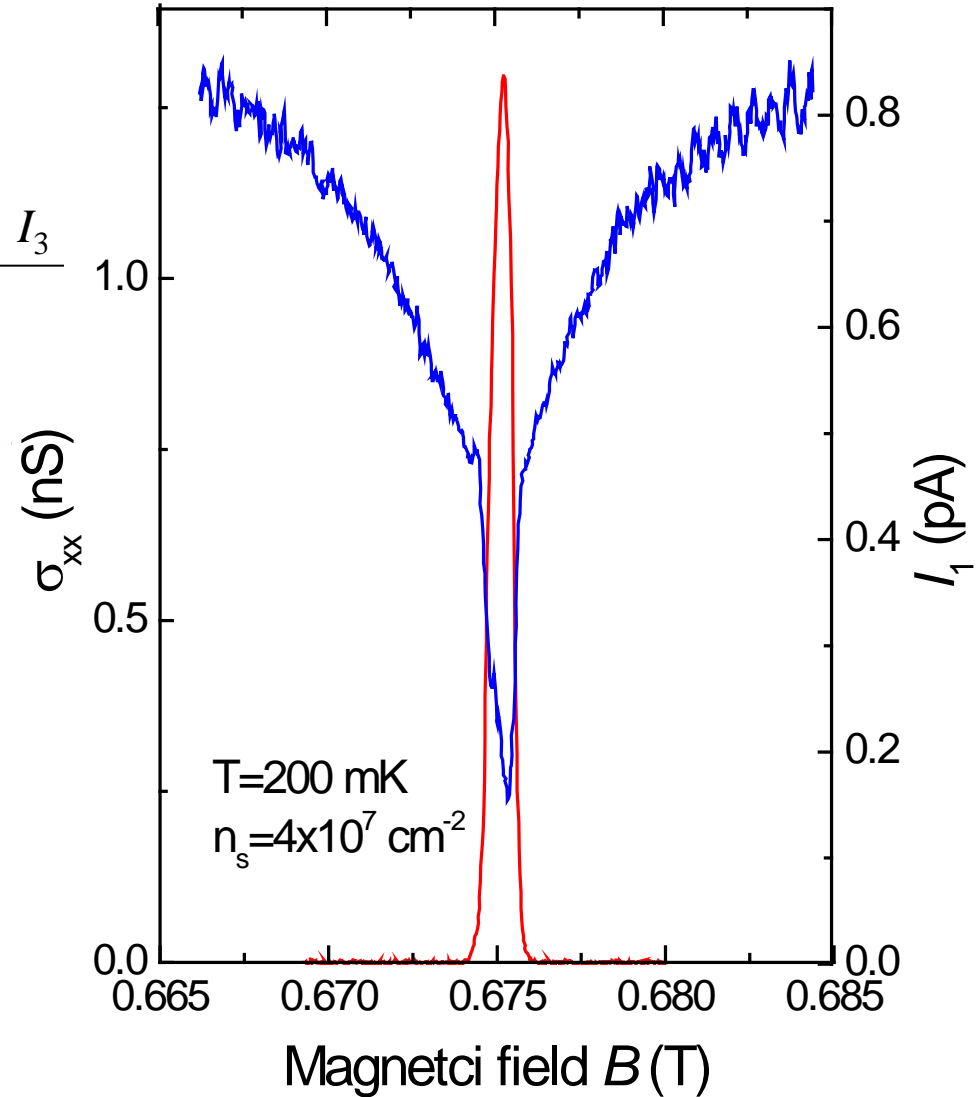
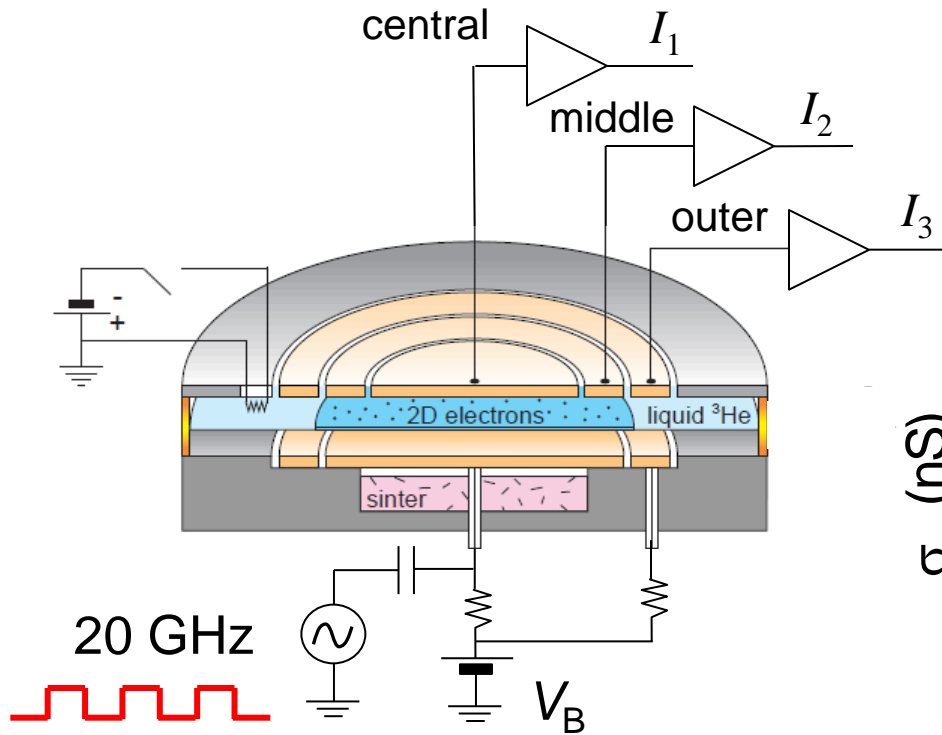
Badrutdinov, Abdurakhimov, DK, PRB 90, 075305 (2014)

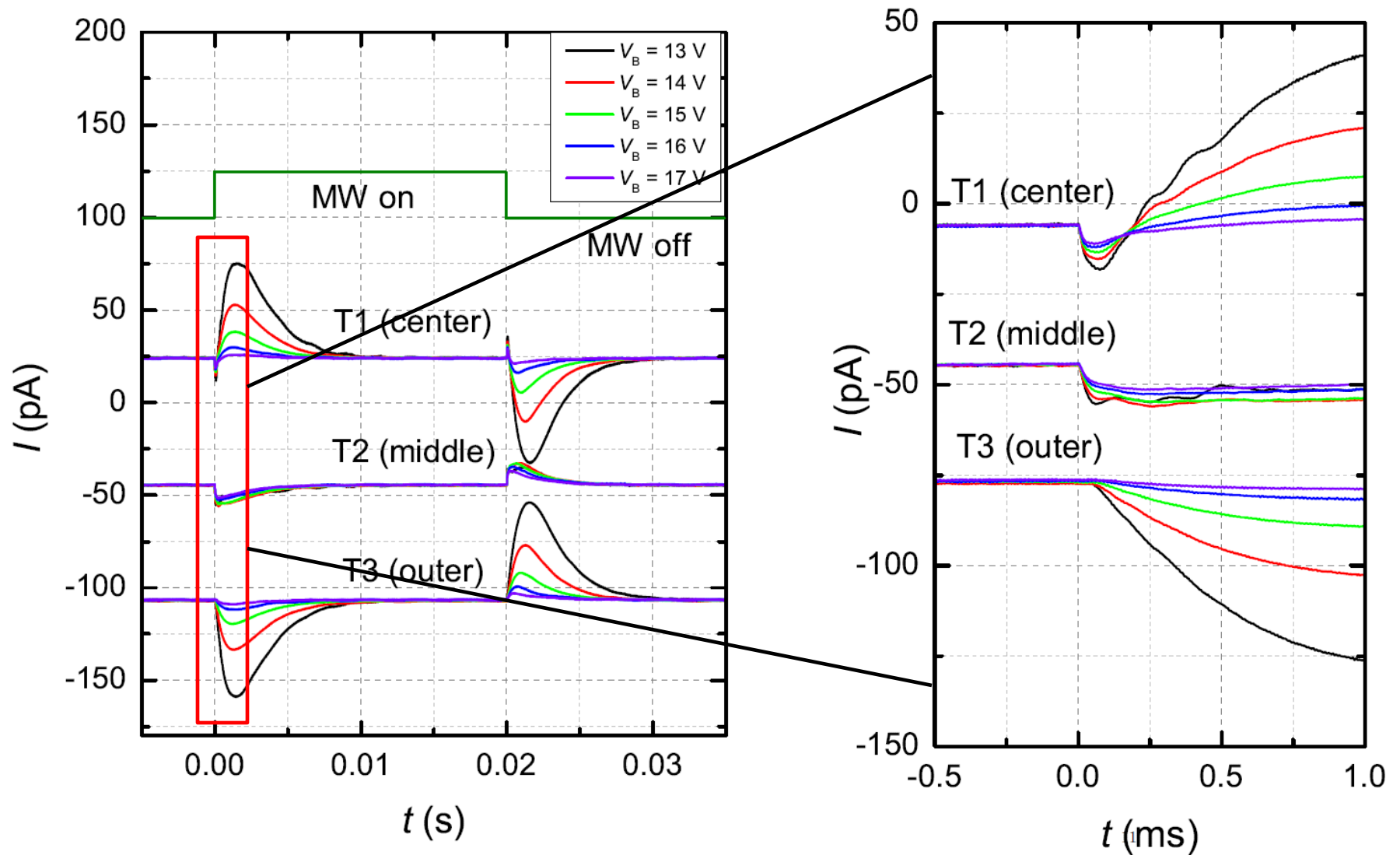


Irreversible loss of electrons
at high MW power

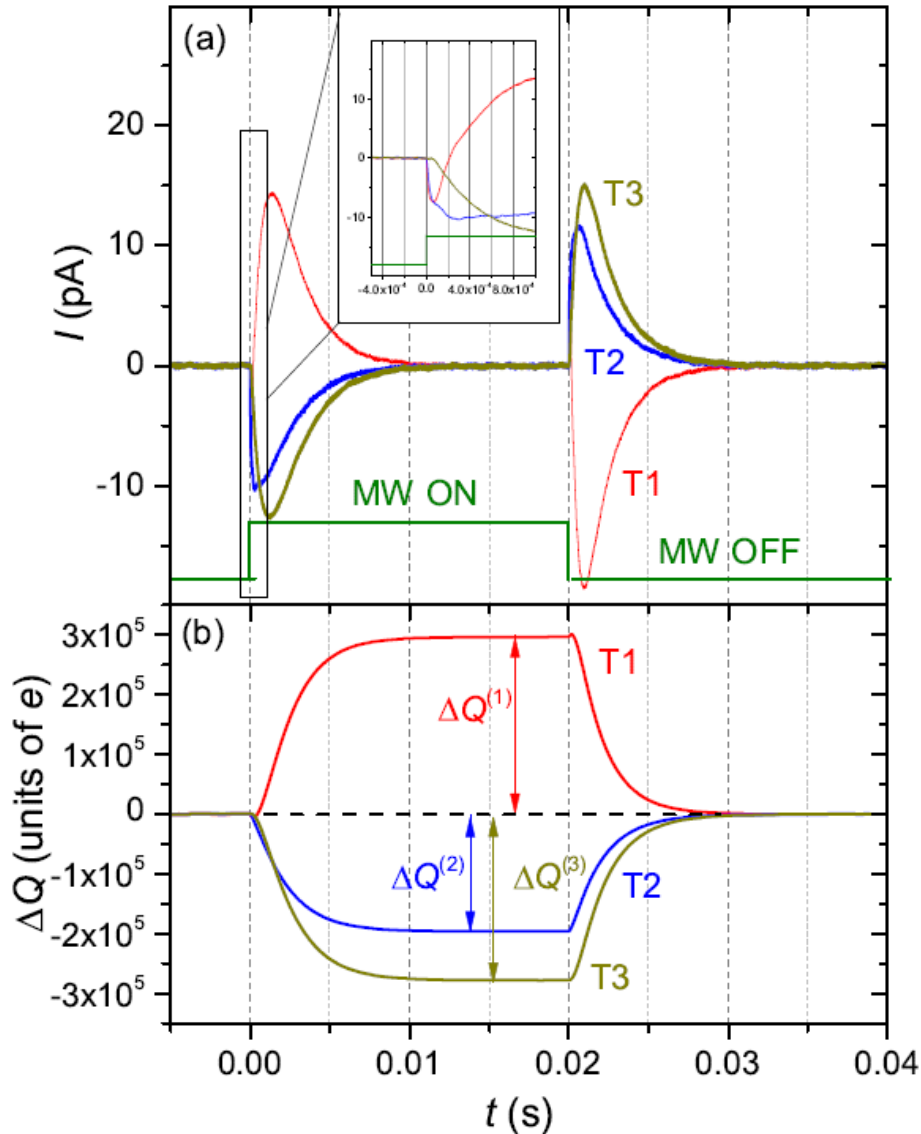


Badrutdinov, Abdurakhimov, DK, PRB 90, 075305 (2014)





Badrutdinov, Abdurakhimov, DK, PRB 90, 075305 (2014)



Extraction of $\Delta Q_{\text{perp}}^{(i)}$ and $\Delta Q_{\text{in-plane}}^{(i)}$ from data:

$$\Delta Q^{(i)} = \Delta Q_{\text{in-plane}}^{(i)} + \Delta Q_{\text{perp}}^{(i)}$$

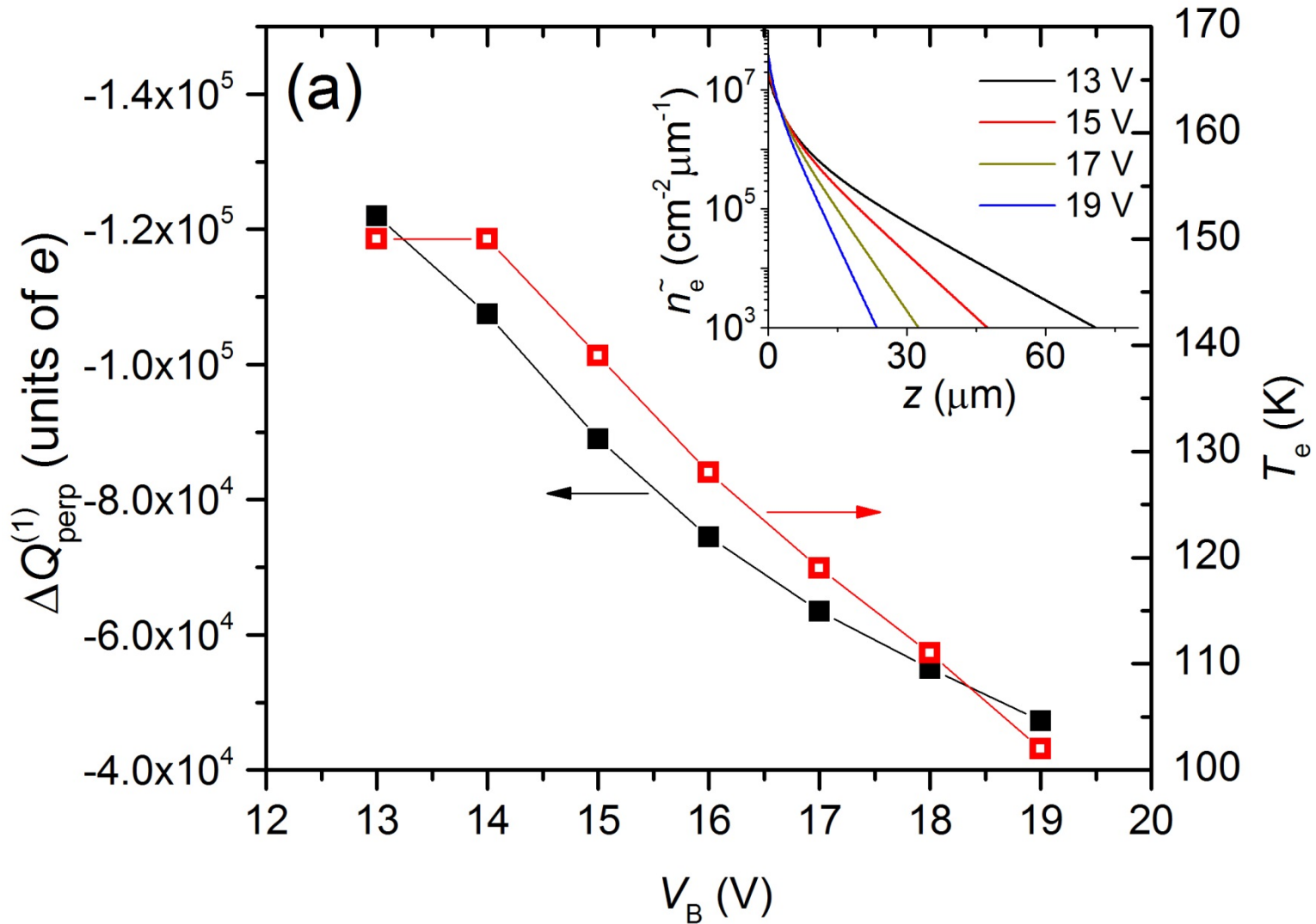
$$\Delta Q_{\text{in-plane}}^{(1)} + \Delta Q_{\text{in-plane}}^{(2)} + \Delta Q_{\text{in-plane}}^{(3)} = 0$$

$$\Delta Q_{\text{perp}}^{(1)} = \Delta Q_{\text{perp}}^{(2)}$$

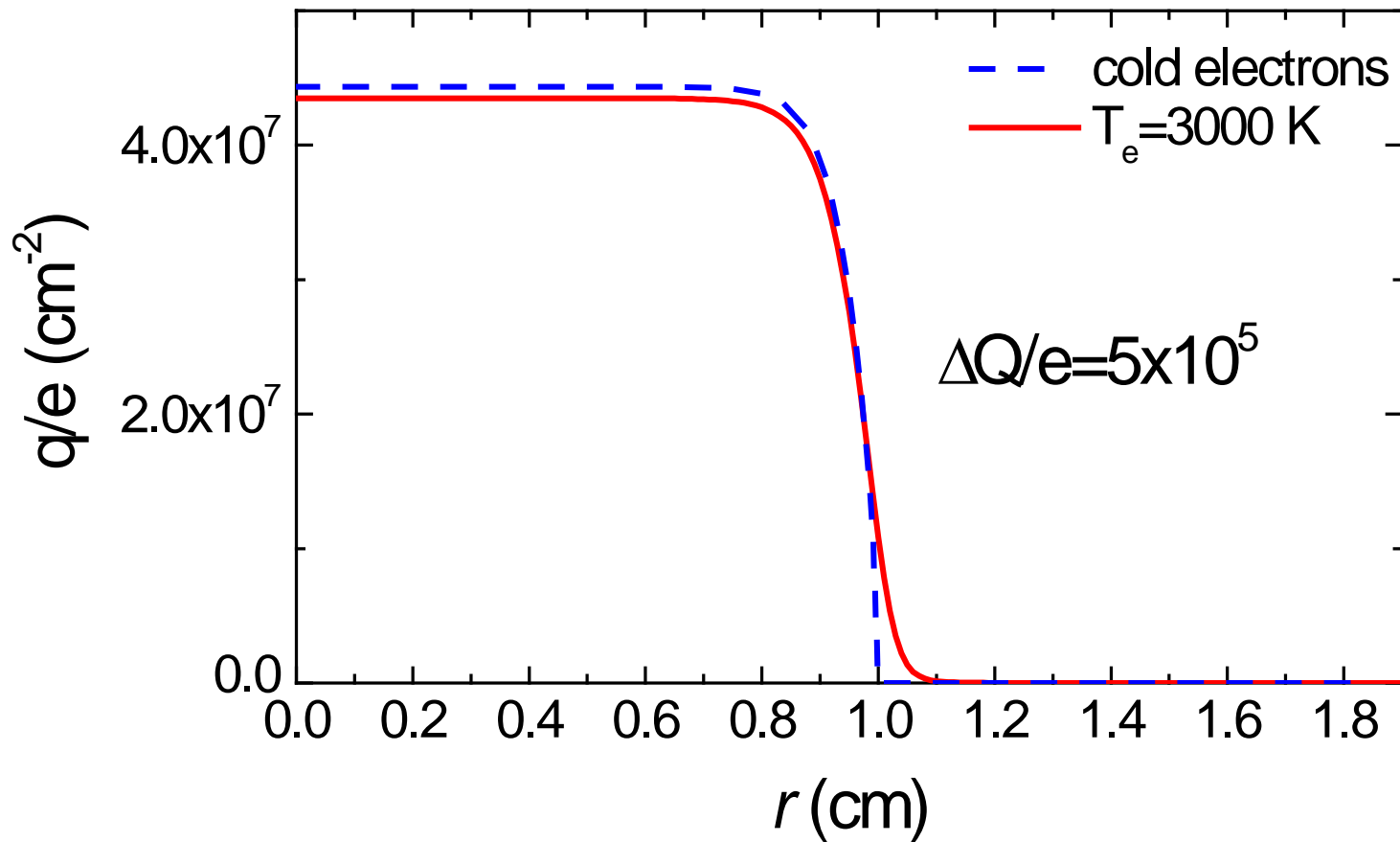
$$\Delta Q_{\text{perp}}^{(3)} = 0$$

V_B (v)	$\Delta Q_{\text{in-plane}}^{(1)}$	$\Delta Q_{\text{in-plane}}^{(2)}$	$\Delta Q_{\text{in-plane}}^{(3)}$	ΔQ_{perp}
13	-1338000	55000	1283000	122000
14	-736500	109500	627000	107500
15	-385000	107000	278000	89000
16	-184500	72500	112000	74500
17	-95500	46500	49000	63500
18	-56800	32000	24800	55000
19	-38600	23700	14900	47300

$$Q_0 = 1.35 \cdot 10^8$$

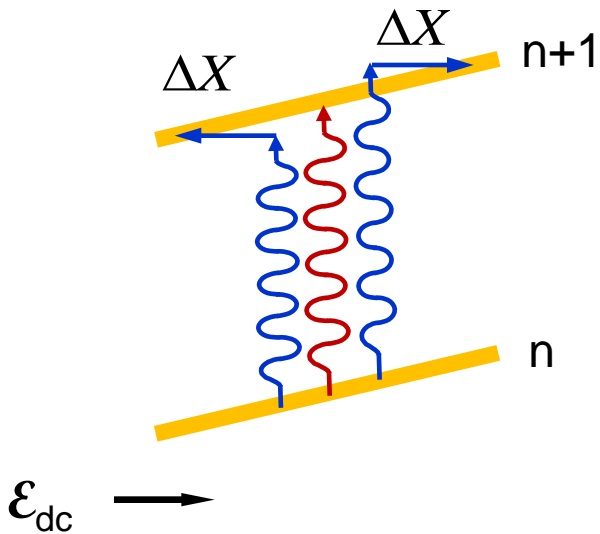


Simultaneous solution of Poisson and Boltzmann equation gives estimate of **3,000 K** for electron temperature

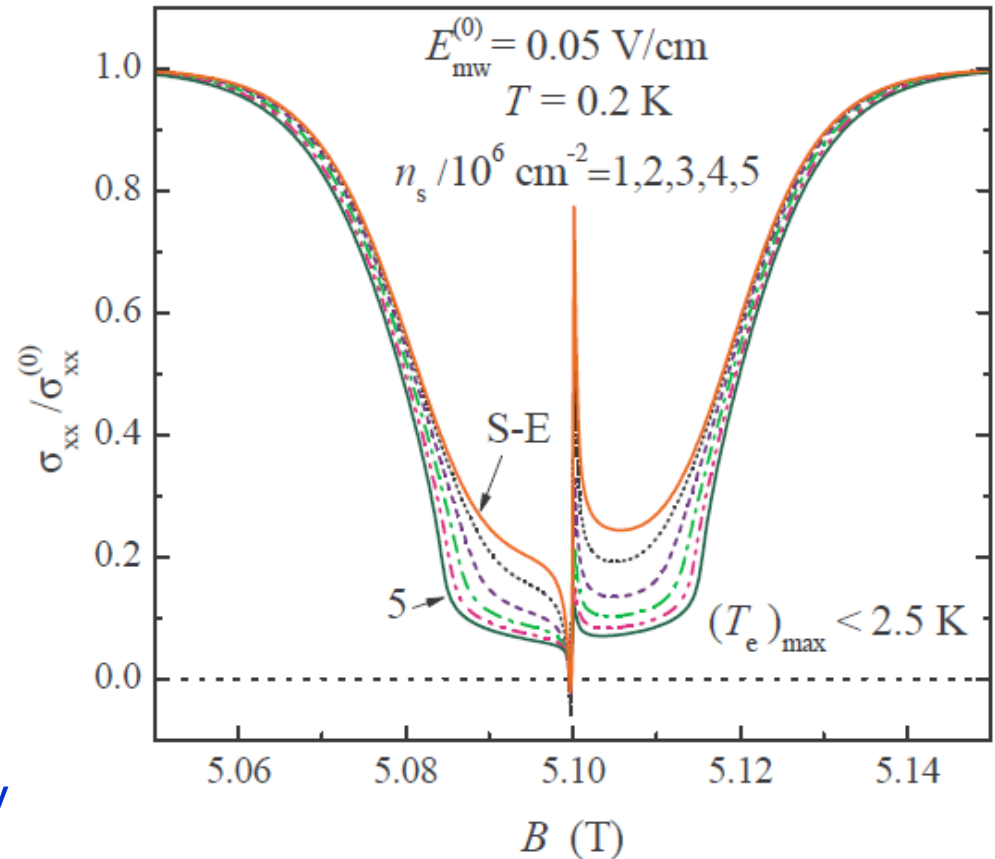


Breakdown of the effective electron temperature approximation?

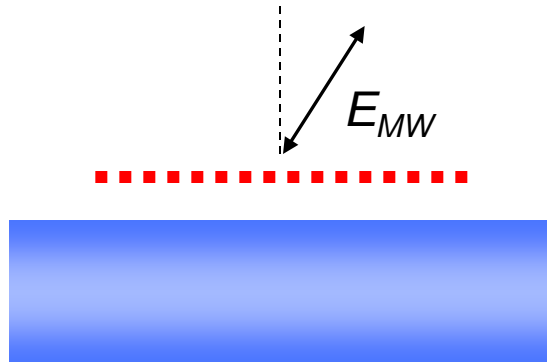
Yu. Monarkha, *PRB(R)* 2015



Predicts negative σ_{xx} and instability
on the low-field side of CR

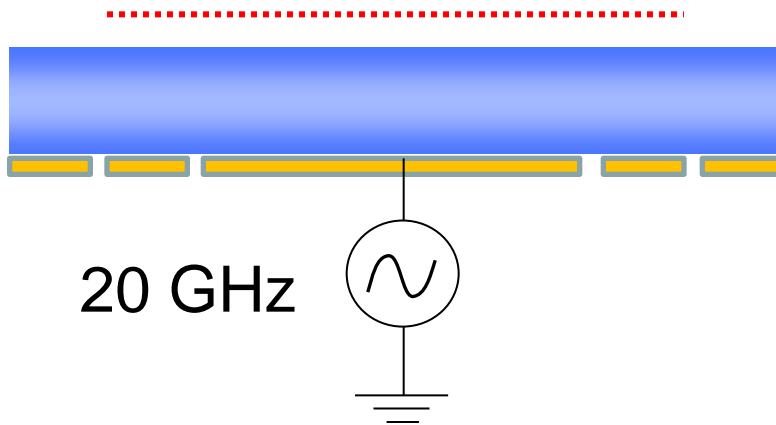


Magarill and Entin, arXiv:1504.03422



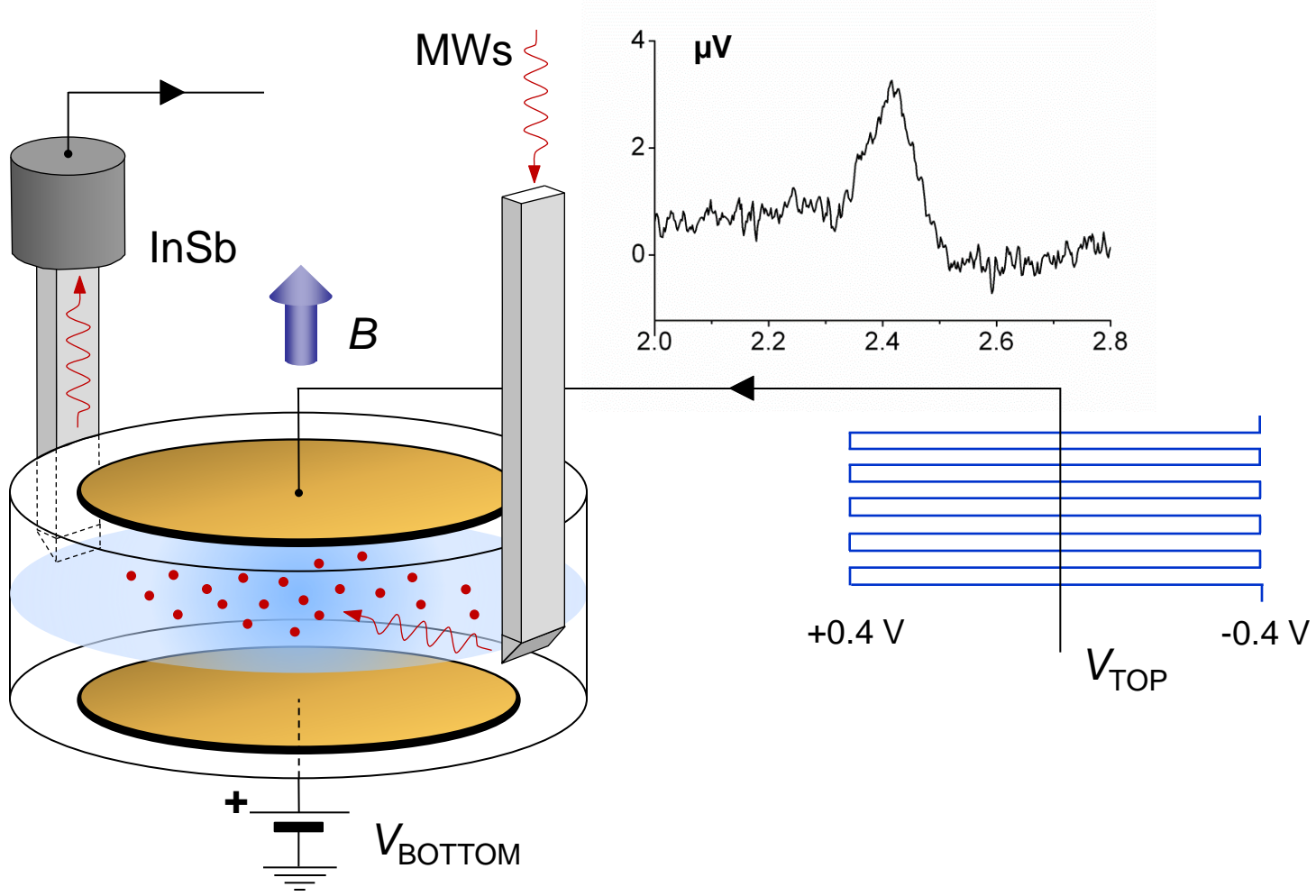
$$j_x = \left\langle en_s \sum_{\beta'} (X_{\beta'} - X_{\beta}) w_{\beta \rightarrow \beta'} \right\rangle$$

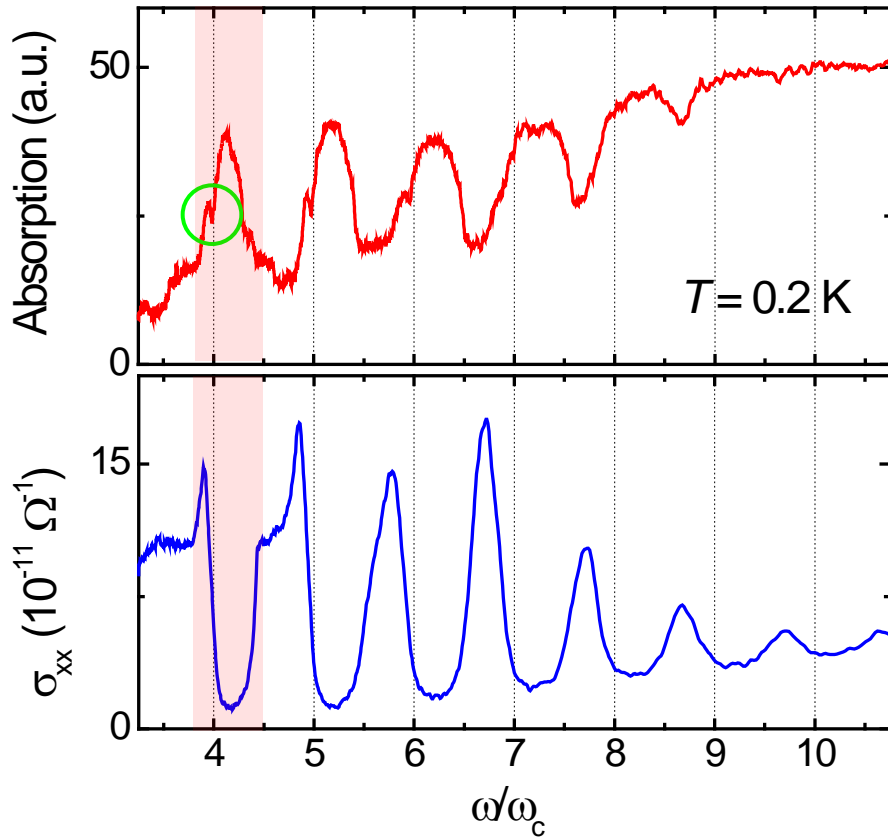
Second order perturbation theory



Would expect radial photocurrent
in our geometry

- In principle, our observation is consistent with formation of a quasy-3D electron system speculated earlier.
- However, it is difficult to understand why different motional degrees of freedom do not thermalize.
- Other theoretical proposals might be relevant but require examination

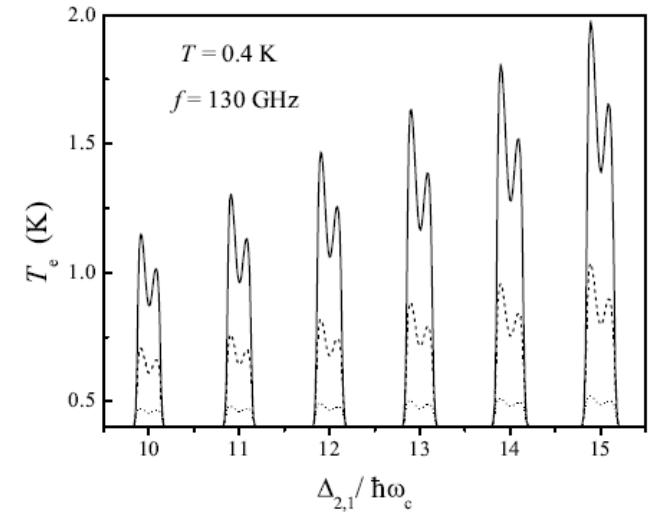


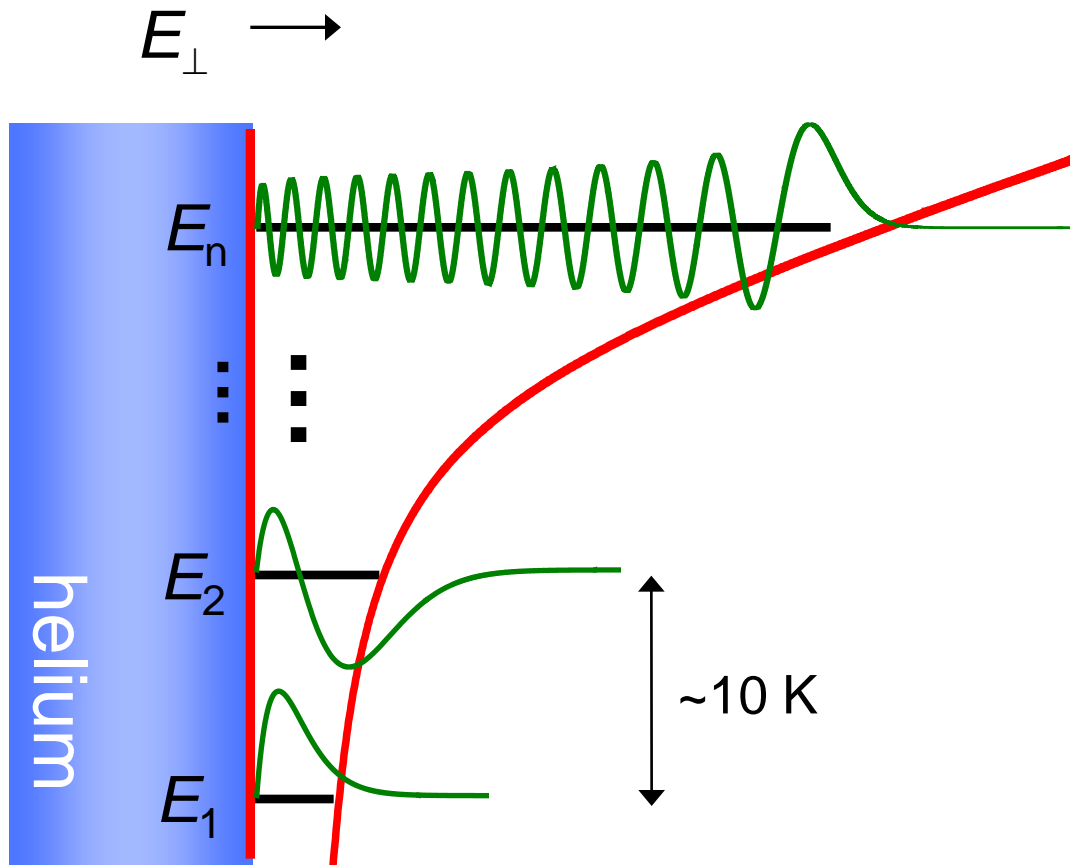


Energy balance equation:

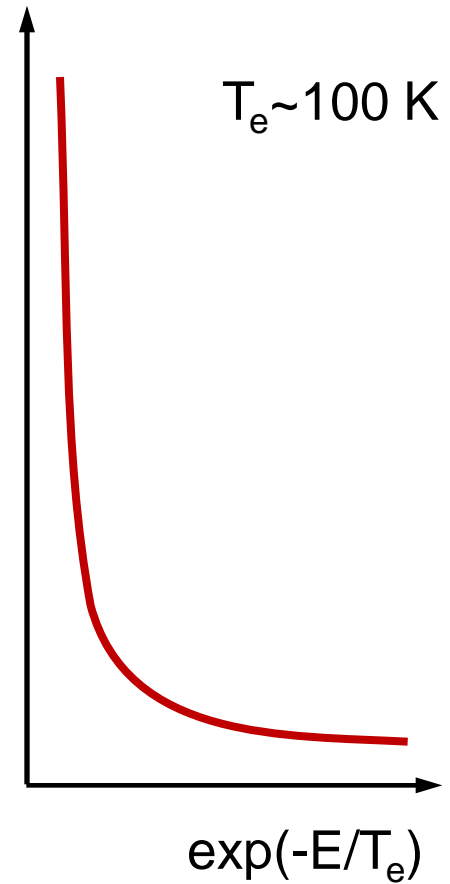
$$\text{Absorption} = \nu_E \cdot (T_e - T)$$

Heating of electrons:





2D system below 1 K



Quasy-3D hot electron system