

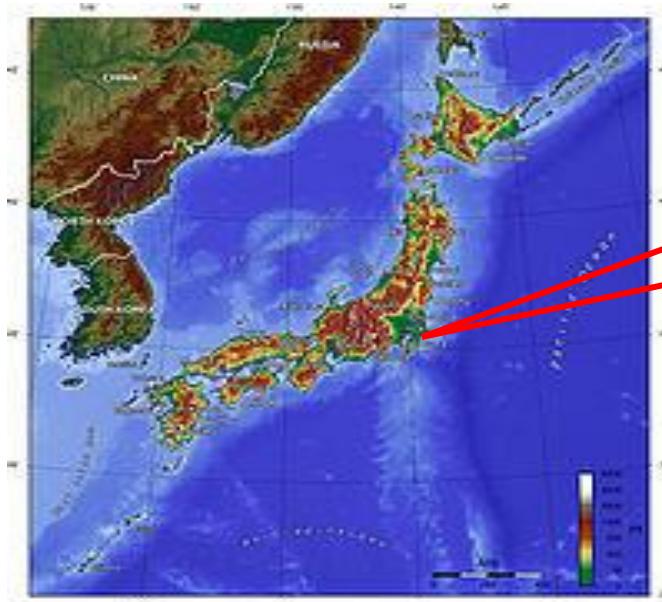
New Quantum Phenomena in Electrons on Helium under Microwave Excitation

Denis Konstantinov
Quantum Dynamics Unit
OIST Graduate University



理化学研究場

RIKAGAKUKENKYUJYO - RIKEN

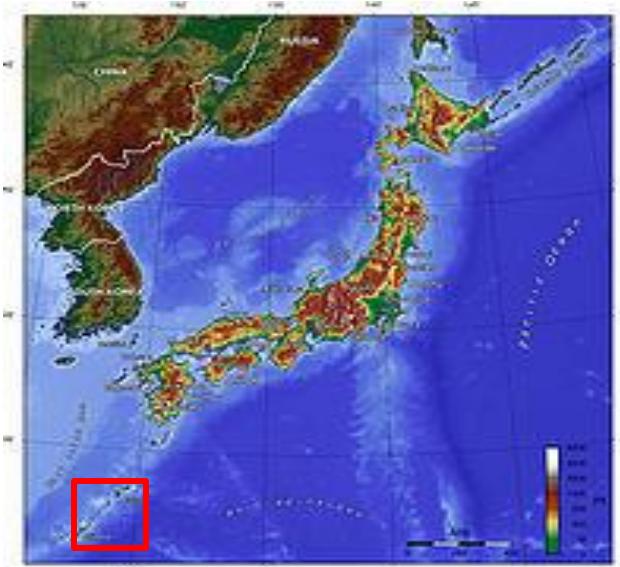


Wako campus

- Japan's largest research institute
- Over 3,000 researchers
- Largest campus - 15 min from downtown Tokyo



Okinawa Institute of Science and Technology - OIST



- 45 Research Units in Neuroscience, Biology, Physics and Chemistry
- No divisions into departments
- 350 researchers (approximately half are not Japanese)
- Graduate University since 2013

Experiment

Kimitoshi Kono, RIKEN

Hanako Isshiki, RIKEN

Hikota Akimoto, RIKEN

Alexei Chepelianskii, University Paris-Sud

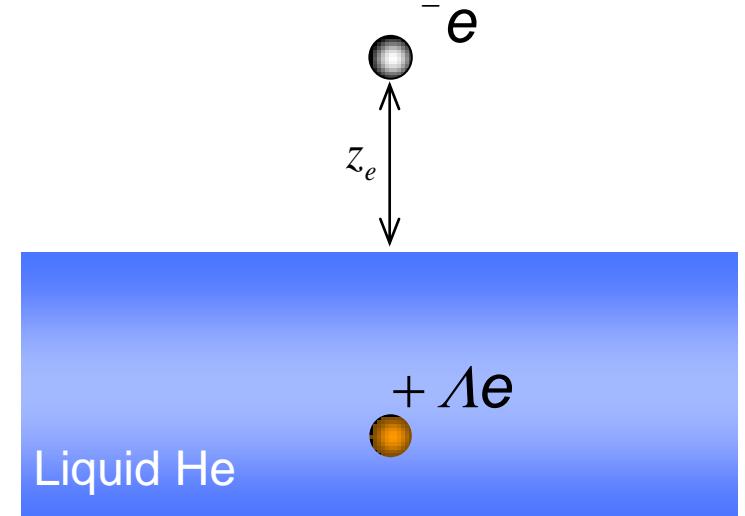
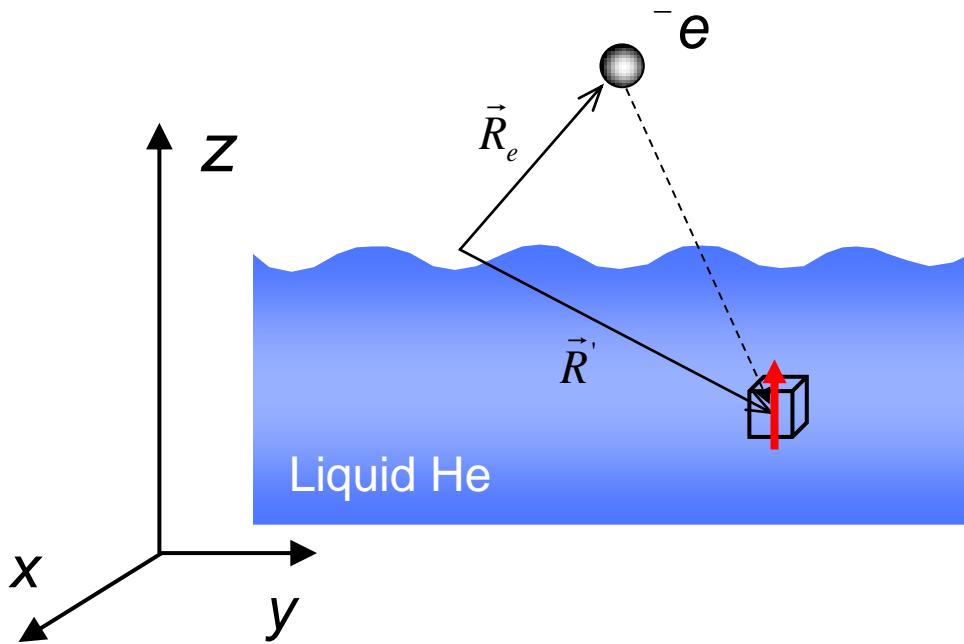
Masa Watanabe, RIKEN

Theory

Yuriy Monarkha, ILTPE, Kharkov

Mark Dykman, Michigan State University

- Electrons on helium versus 2DEG in semiconductors
- Recent interests
- Electrons under microwave excitation
- Microwave-induced **Zero-Resistance States (ZRS)**
- Future directions



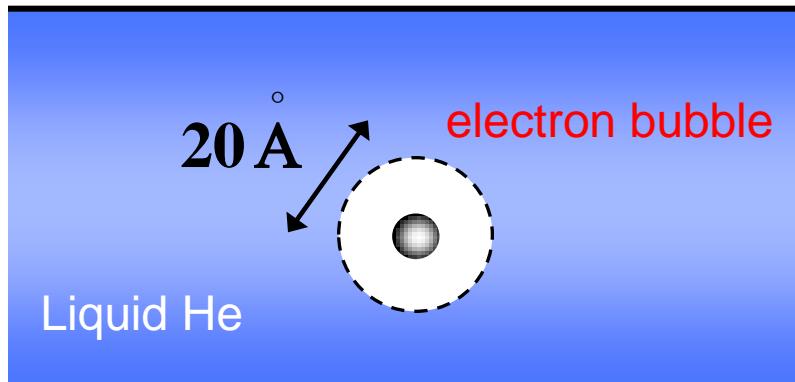
$$U_{pol}(\vec{R}_e) = -\frac{(\varepsilon - 1)e^2}{4(\varepsilon + 1)} \int d^3 \vec{R} \frac{1}{|\vec{R} - \vec{R}_e|^4}$$

$$U_{pol}(z_e) = -\frac{\Lambda e^2}{z_e},$$

$$\Lambda = \frac{(\varepsilon - 1)}{4(\varepsilon + 1)} \approx 0.005$$

$-e$

Potential barrier ~ 1 eV



The Pauli exclusion principle -
electron avoids He atoms

Sommer, 1964

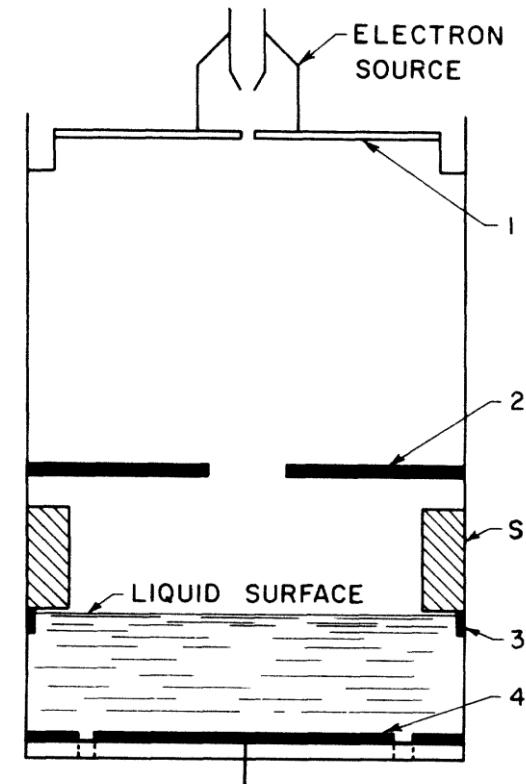
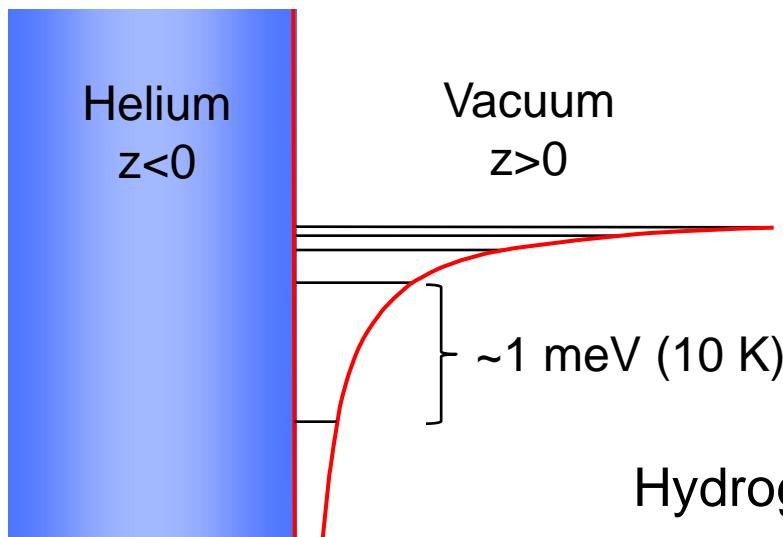


FIG. 1. The experimental chamber.

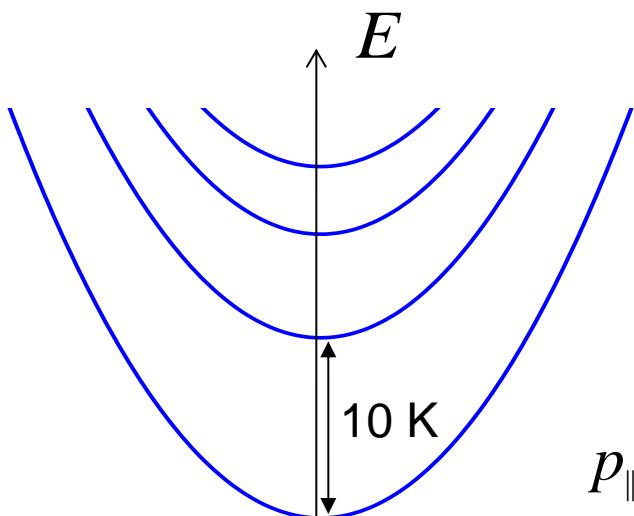


Equation of motion in z -direction:

$$\psi_n''(z) + \left(\frac{2mE_n}{\hbar^2} + \frac{\alpha}{z} \right) \psi_n(z) = 0$$

Hydrogen-like spectrum:

$$E_n = -\frac{Ry}{n^2}$$

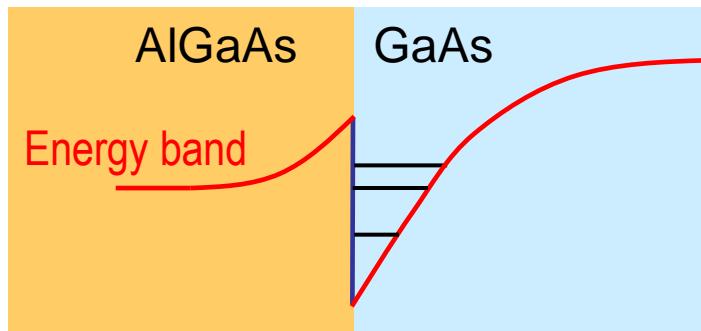


Total energy:

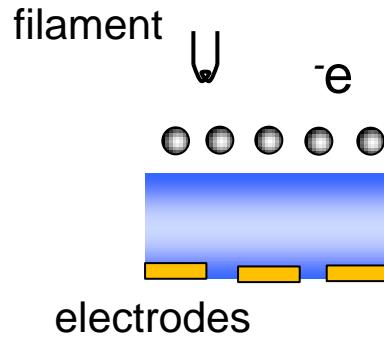
$$E = E_n + \frac{p_{||}^2}{2m} \pm \underbrace{\mu_B B_{||}}_{\text{due to spin}}$$

$\underbrace{\qquad\qquad\qquad}_{\text{2D motion}}$

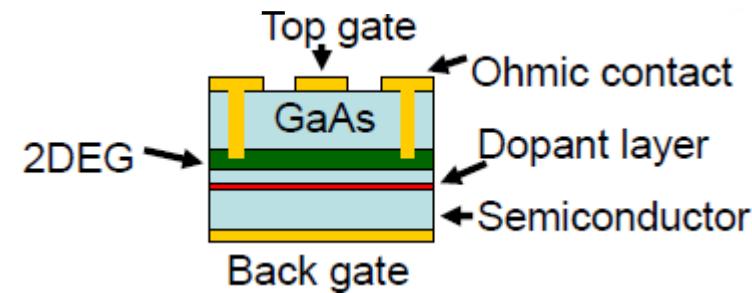
Comparison with traditional 2DES



Complement to degenerate 2DEG in
Si MOSFETs and GaAs heterostructures



- Liquid/Superfluid interface
- Dielectric constant $\epsilon = 1$
- Effective mass = $1.0 m_e$
- g-factor = 2
- Electron density $n_s < 2 \times 10^9 \text{ cm}^{-2}$
Limited by surface instability!



- Crystalline interface
- Dielectric constant $\epsilon = 10$
- Effective mass = $0.067 m_e$
- g-factor = -0.44
- Electron density $n_s > 5 \times 10^{10} \text{ cm}^{-2}$

Relevant energies

$$r_p = \frac{V_C}{E_f} = \frac{e^2 \sqrt{\pi n_s}}{4\pi\epsilon\epsilon_0} \frac{m^*}{\hbar^2 \pi n_s}$$

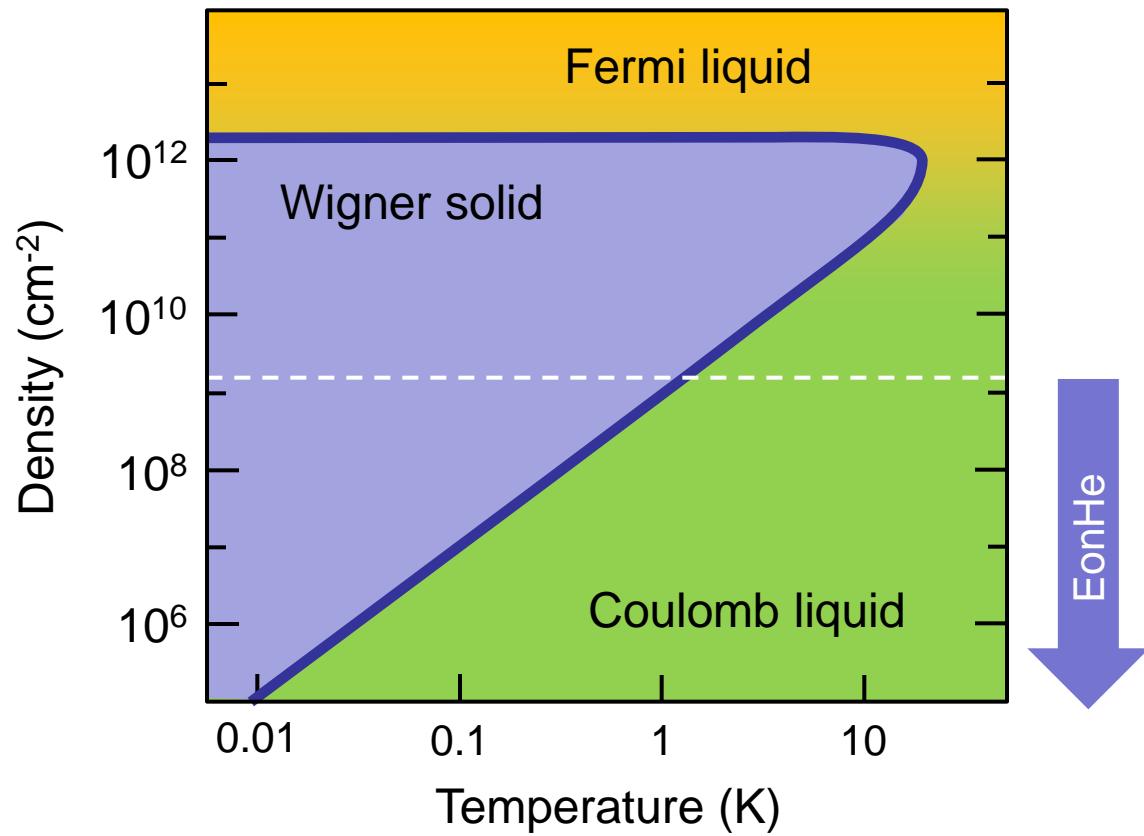
Quantum fluctuations

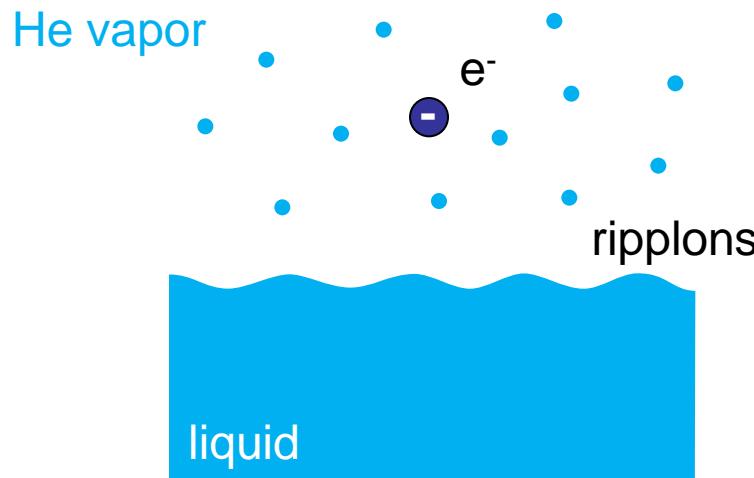
$$\Gamma_p = \frac{V_C}{E_{th}} = \frac{e^2 \sqrt{\pi n_s}}{4\pi\epsilon\epsilon_0 k_B T}$$

Thermal fluctuations

Typical electron densities

$$n_s < 2 \times 10^9 \text{ cm}^{-2}$$





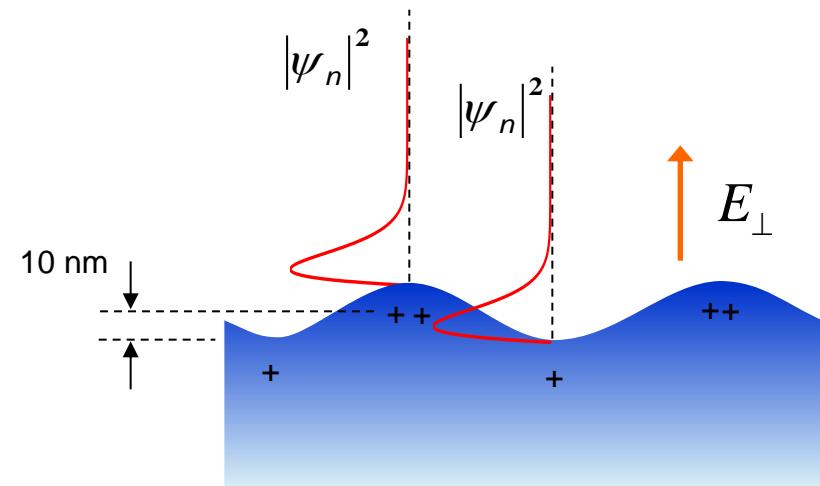
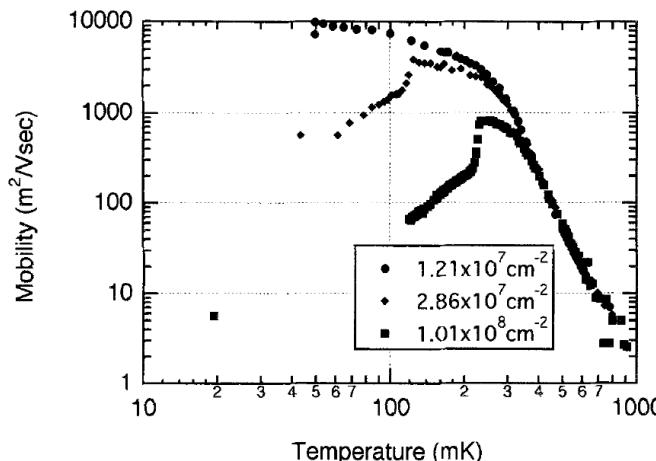
- Scattering at helium vapor atoms

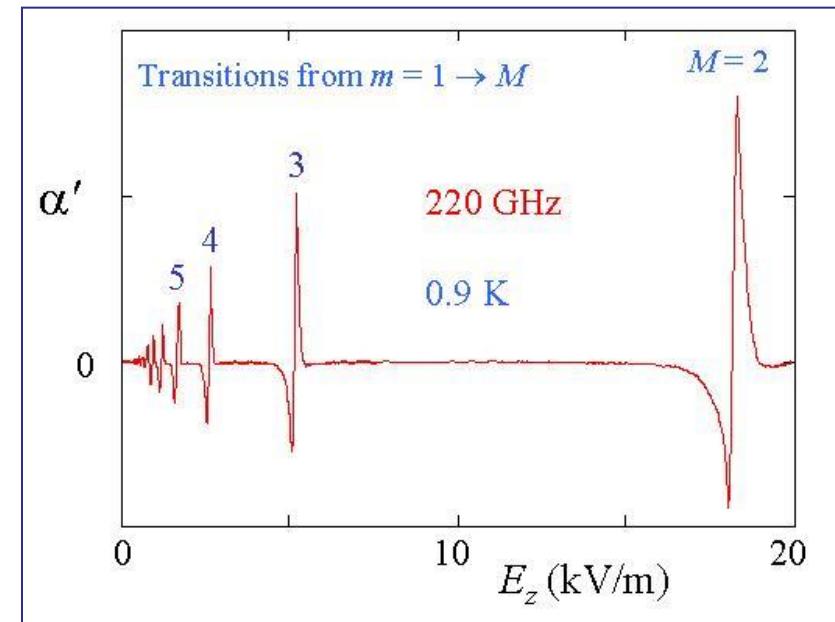
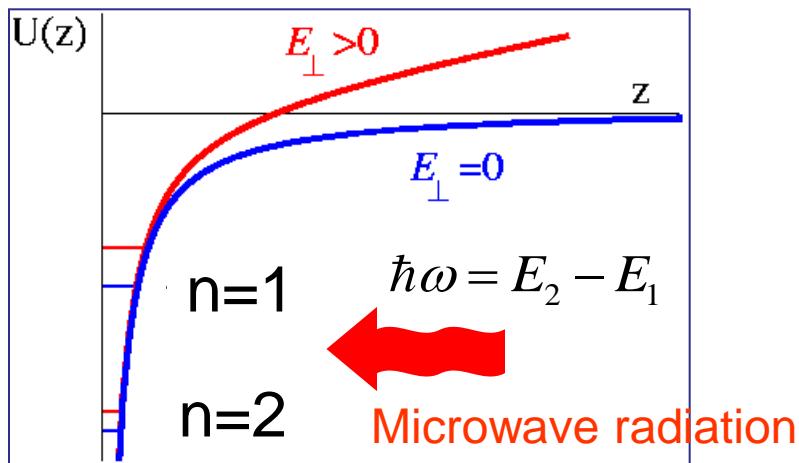
$$N_{vapor} \propto T^{3/2} \exp\left(-\frac{Q}{T}\right)$$

- Scattering at surface waves (ripplons)

$$N_q = \frac{1}{\exp\left(\frac{\hbar\omega_q}{k_B T}\right) - 1} \propto T$$

Highest mobility known!





Interesting many-body physics

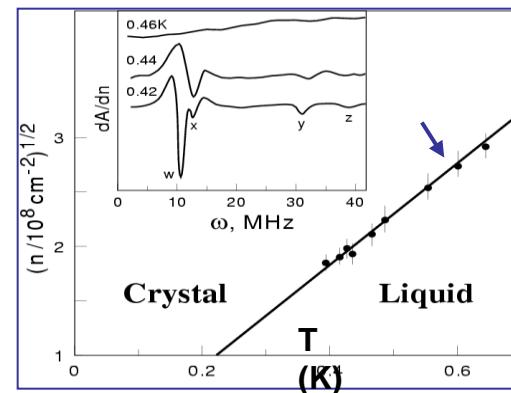
- Coupled plasmon-riplon modes

Grimes and Brown, Platzman

- Edge magneto-plasmons

Dahm, Williams, Glattli, Lea

C.C.Grimes & Brown
PRL 32, 280 (1974)



Grimes & Adams,
PRL 42, 795 (1979)

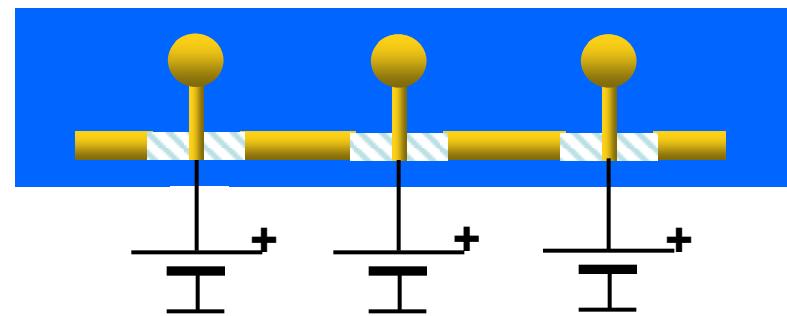
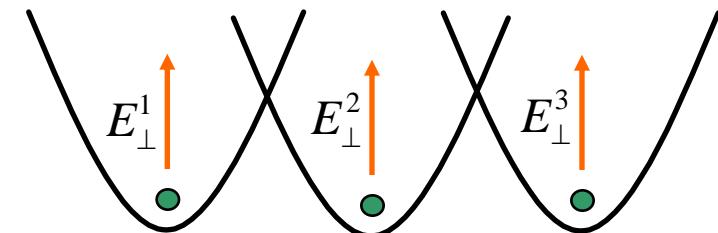
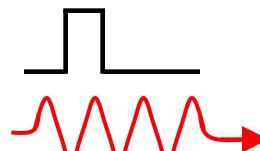
SCIENCE VOL 284 18 JUNE 1999

Quantum Computing with Electrons Floating on Liquid Helium

P. M. Platzman^{1*} and M. I. Dykman²

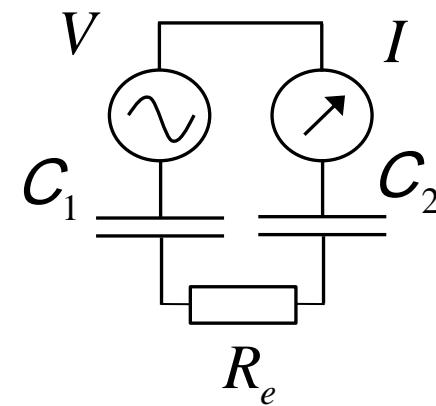
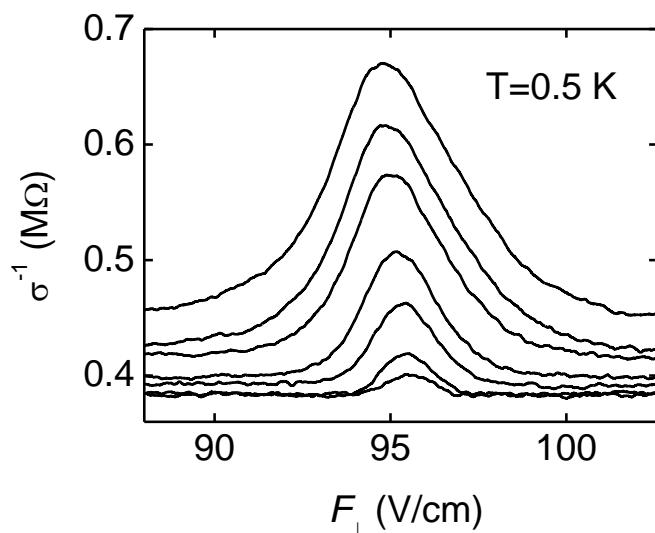
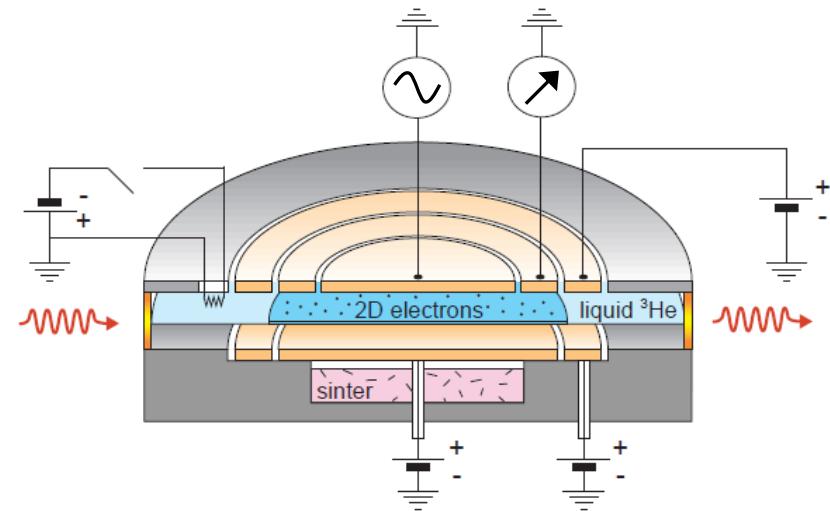
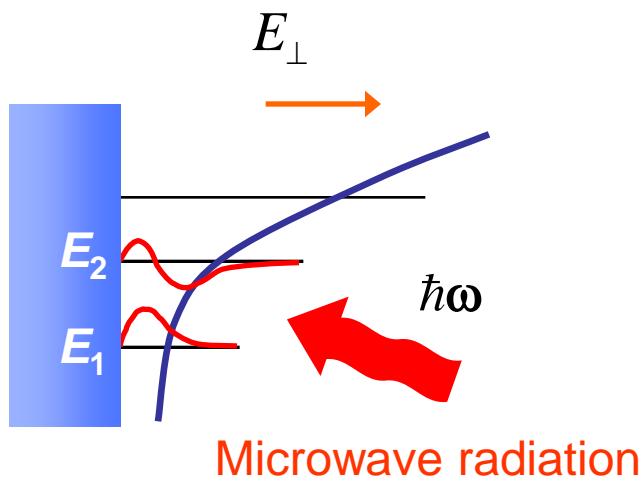
A quasi-two-dimensional set of electrons ($1 < N < 10^9$) in vacuum, trapped in one-dimensional hydrogenic levels above a micrometer-thick film of liquid helium, is proposed as an easily manipulated strongly interacting set of quantum bits. Individual electrons are laterally confined by micrometer-sized metal pads below the helium. Information is stored in the lowest hydrogenic levels. With electric fields, at temperatures of 10^{-2} kelvin, changes in the wave function can be made in nanoseconds. Wave function coherence times are 0.1 millisecond. The wave function is read out with an inverted dc voltage, which releases excited electrons from the surface.

mm-MW pulse

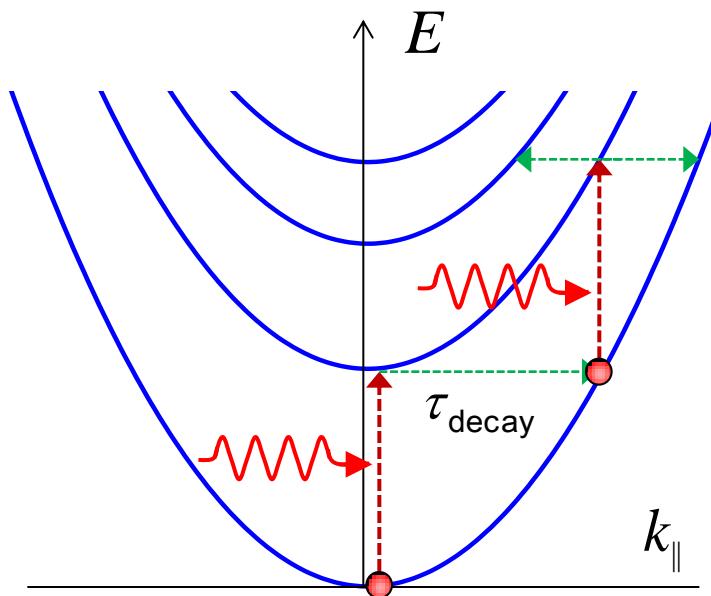


$T_1 = 100 \mu\text{s}$

- Identification of well-defined qubits:
 $|I0\rangle$ and $|I1\rangle$ states of individual surface electrons
- Reliable state preparation:
Below 1 K almost all qubits will be in the quantum ground state $|I0\rangle$
- Low decoherence
- Scalability!



Sommer-Tanner method

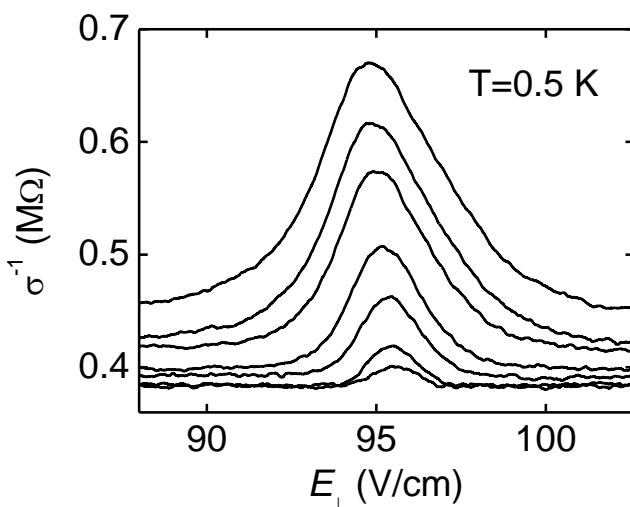


2D energy subbands

$$E = E_n + \frac{\hbar^2 k_{\parallel}^2}{2m}$$

Decay due to elastic scattering

$$\tau_{\text{decay}} \approx 10^{-9} - 10^{-8} \text{s}$$



Very fast thermalization $T_e \gg T$

$$\tau_{ee} \sim \omega_p \approx 10^{-11} \text{s}$$

Cooling due to inelastic scattering

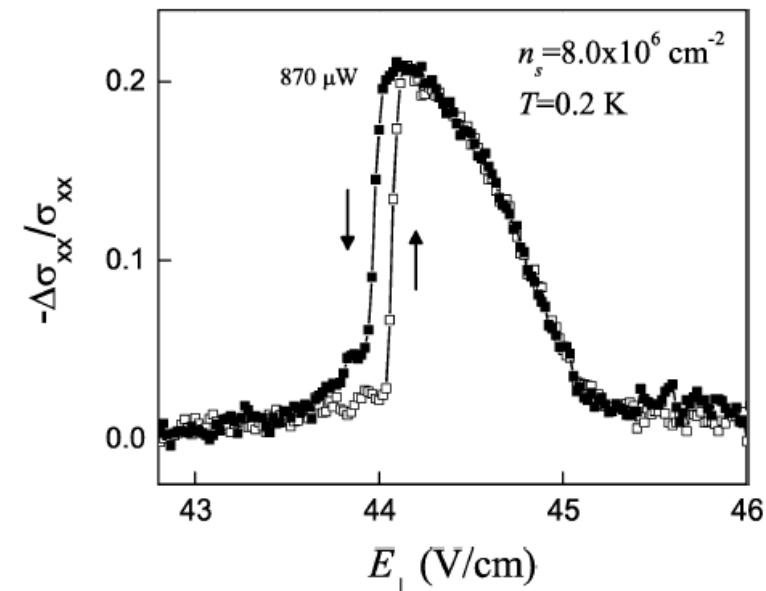
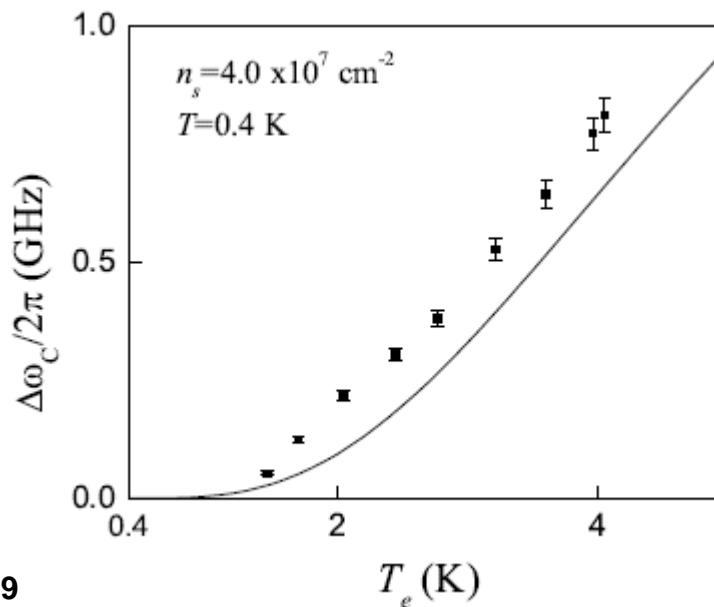
$$\tau_E \approx 10^{-4} - 10^{-6} \text{s}$$

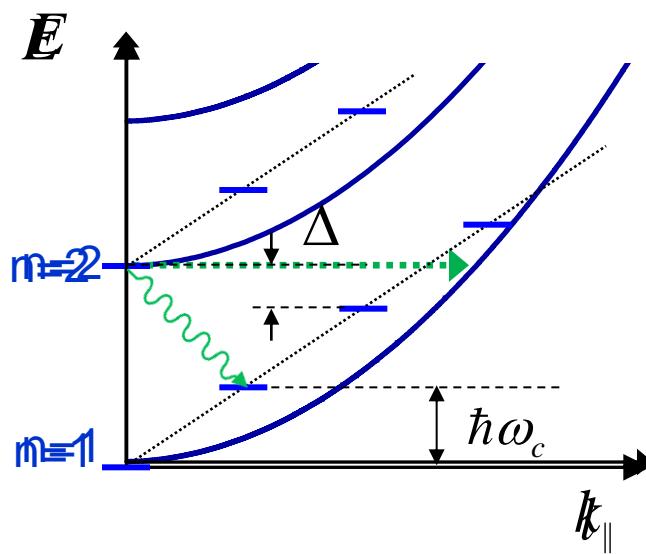
Estimate using mean-field approximation:

$$\Delta\omega_c = \frac{1}{\hbar} (z_{22} - z_{11}) \times \\ \times \left[\sum_n \rho_n z_{nn} - z_{11} \right] \sum_{c \neq t} \frac{e^2}{|\vec{r}_t - \vec{r}_c|^3}$$



Liquid He





2D energy subbands

$$E = E_n + \frac{\hbar^2 k_{\parallel}^2}{2m}$$

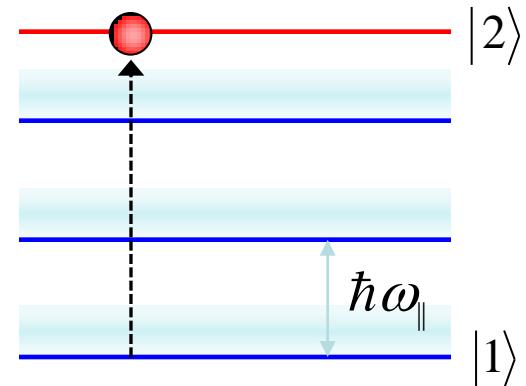
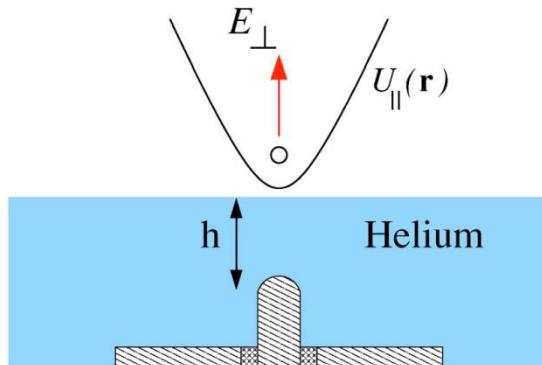
What is we apply magnetic field?

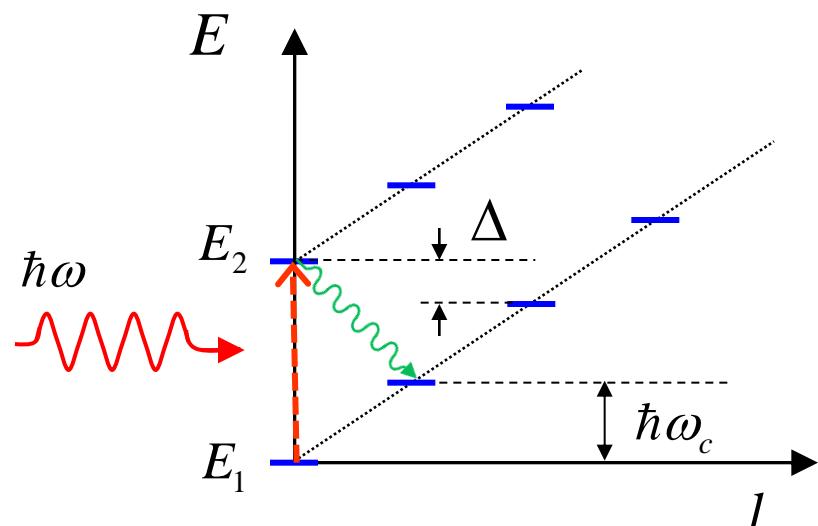
$$E = E_n + \hbar \omega_c (l + 1/2)$$

PHYSICAL REVIEW B **67**, 155402 (2003)

Qubits with electrons on liquid helium

M. I. Dykman,^{1,*} P. M. Platzman,² and P. Sedighrad¹





How do we probe it?

- apply resonant microwaves

$$\hbar\omega = E_2 - E_1$$

- measure DC conductivity

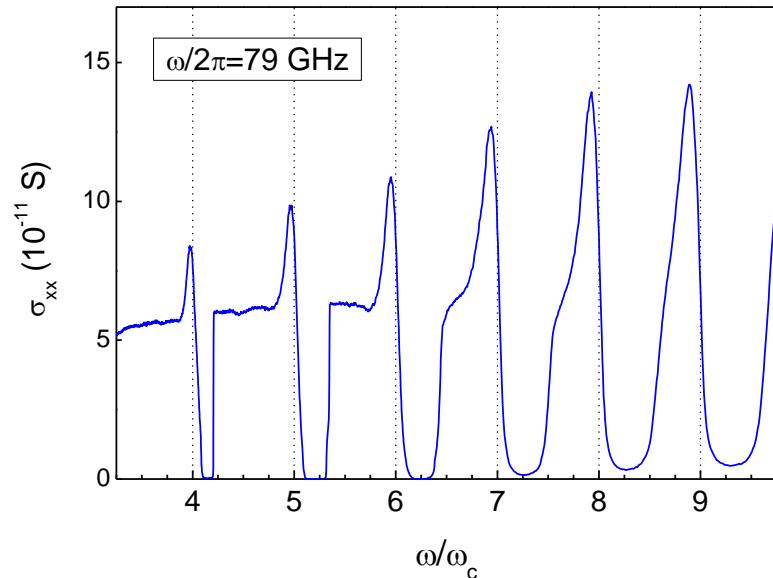
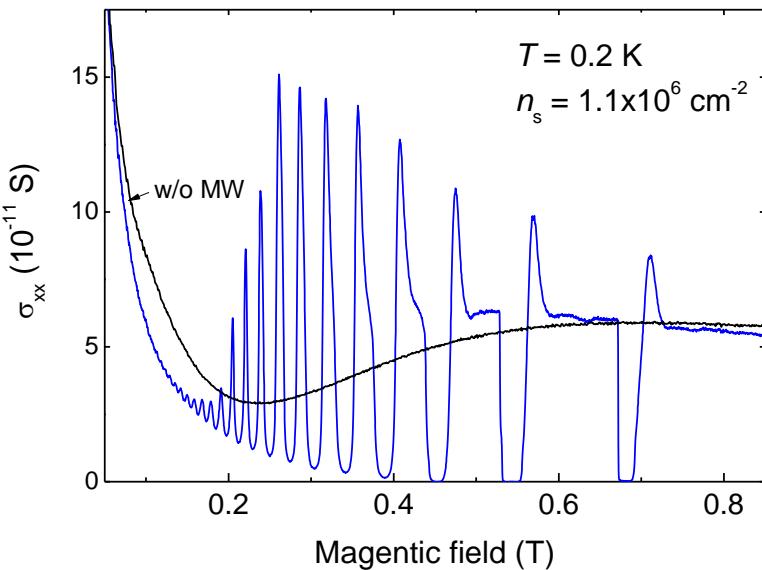
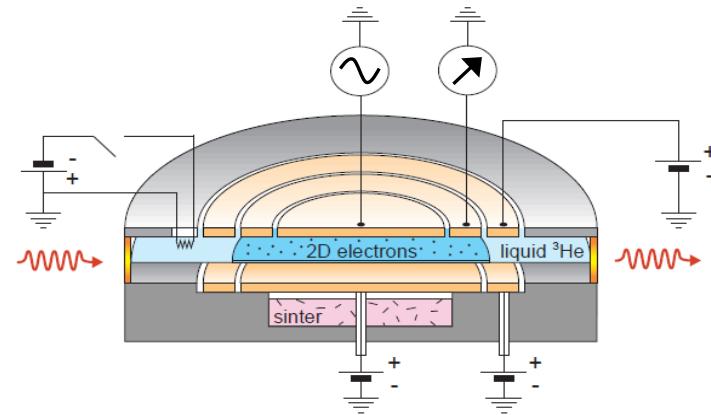
$$\sigma_{xx} = \frac{e^2 n_s v_{eff}}{m_e (\omega_c^2 + v_{eff}^2)}$$

Relaxation dynamics must depend on ratio:

$$\frac{E_2 - E_1}{\hbar\omega_c} = \frac{\omega}{\omega_c}$$

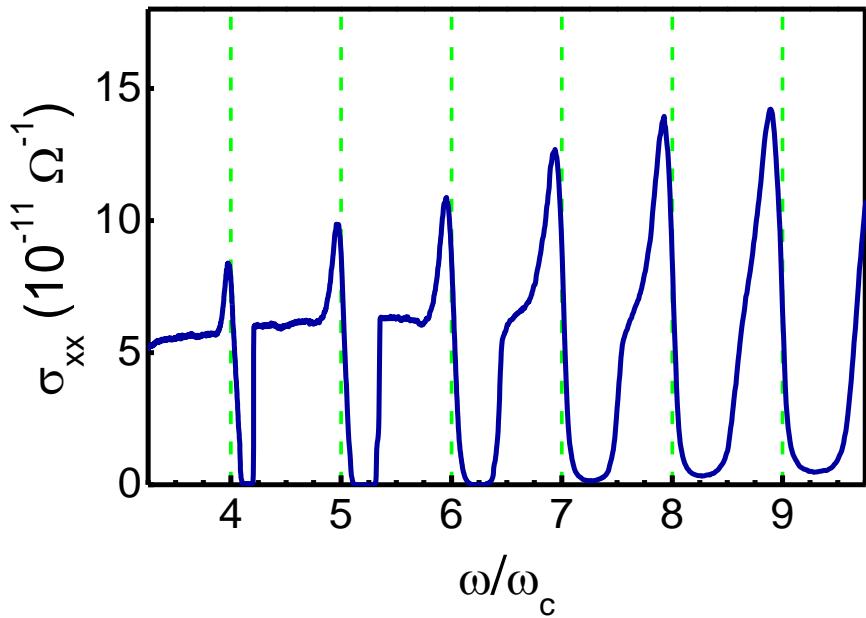
Experimental setup

- Leak-tight copper cell
- Liquid height 1.3 mm
- Kapton windows for MW
- Tuning by Stark shift in perp. electric field



Vanishing conductivity:

$$\sigma_{xx} \rightarrow 0$$



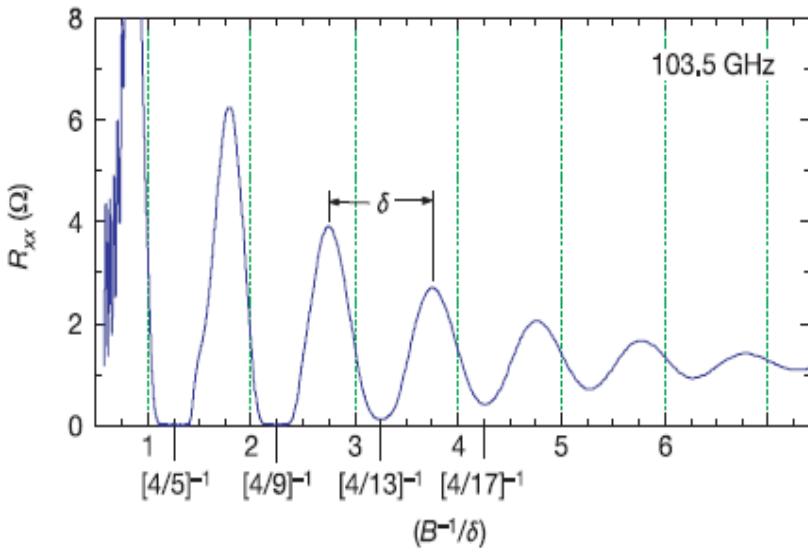
Tensor relation:

$$\rho_{xx} = \frac{\sigma_{xx}}{\sigma_{xx}^2 + \sigma_{xy}^2} \approx \frac{\sigma_{xx}}{\sigma_{xy}^2} \Rightarrow \rho_{xx} \rightarrow 0$$

Vanishing resistance!

Mani et al. Nature 2002

(*highlights in Phys. Today 2003,
Science 2003, Nature 2004*)



Possible explanations:

- Electron pairing due to excitons
(*Nature 2002*)
- Dynamical symmetry breaking
(*PRL 2003, PRB 2009*)
- Disorder-assisted transitions
(*PRL 2003, Nature 2003*)
- Nonequilibrium population of LL
(*PRL 2003, PRB 2003-2010*)
- Microwave stabilization of edge states
(*PRB 2010*)
- Ponderomotive force near contacts
(*PRB 2011*)

Linear transport theory

Yu. P. Monarkha



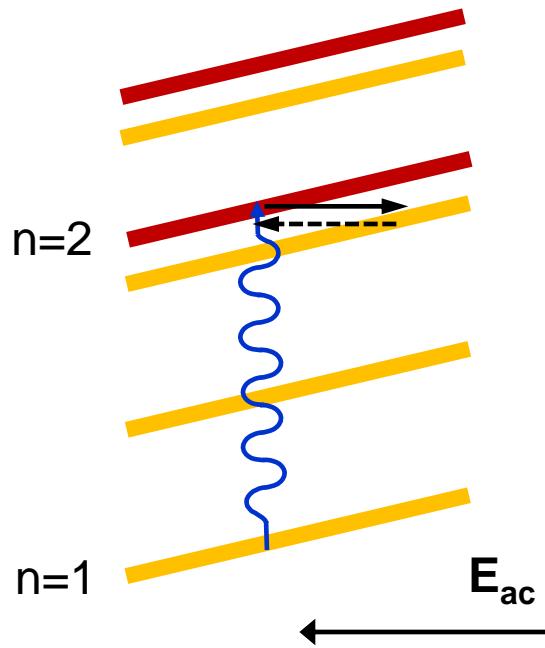
$$\nu_{\text{inter}} \sim \sum_{\mathbf{q}} \hbar \mathbf{q} \sum_{n > n'} \chi_{n,n'}(\mathbf{q}) \cdot \underbrace{S_{n,n'}(q, \omega_{n,n'})}_{\text{DSF}} \cdot (\rho_n + \rho_{n'} e^{-\frac{\hbar \omega_{n,n'}}{k_B T_e}}) +$$

DSF

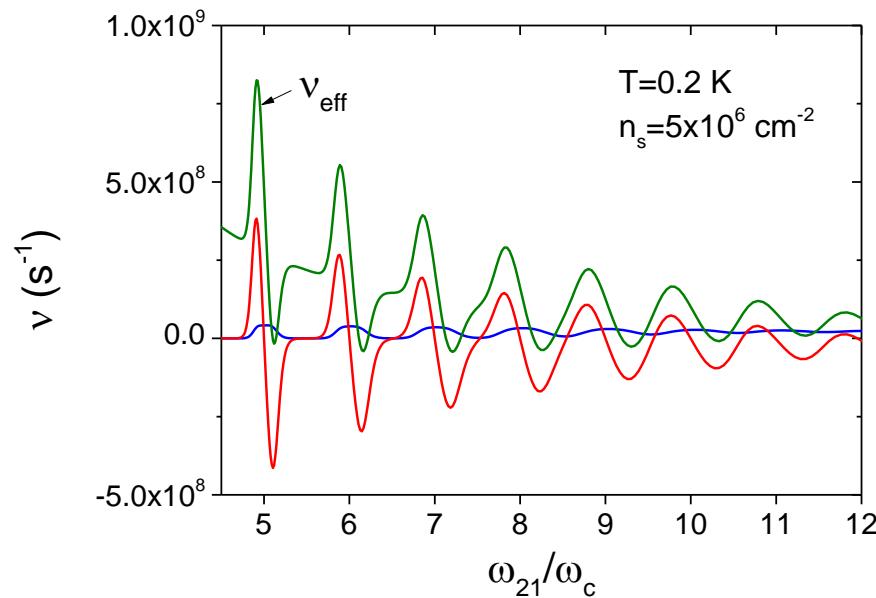
$$+ \frac{\hbar}{k_B T} \sum_{\mathbf{q}} \hbar \mathbf{q} \sum_{n > n'} \chi_{n,n'}(\mathbf{q}) \cdot \underbrace{S'_{n,n'}(q, \omega_{n,n'})}_{\text{derivative of DSF}} \cdot (\rho_n - \rho_{n'} e^{-\frac{\hbar \omega_{n,n'}}{k_B T_e}})$$

derivative of DSF

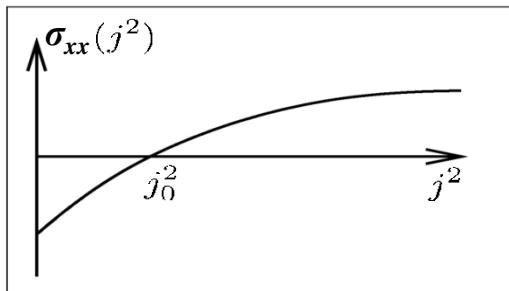
Tilted LL in dc-field



non-zero for nonequilibrium population



There exists (some) mechanism
leading to **absolute negative σ_{xx}**



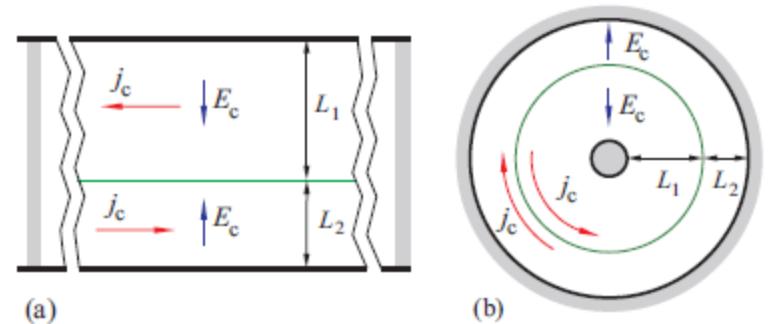
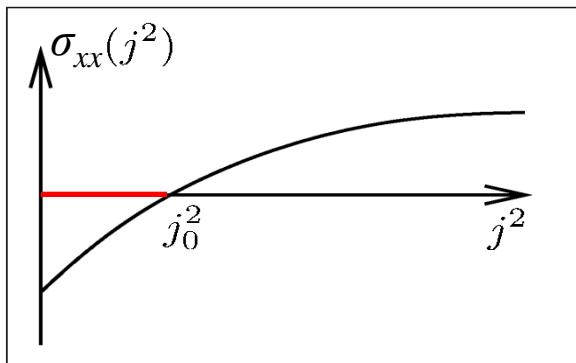
$$\frac{\partial \rho_s}{\partial t} = -\nabla \vec{j} = \sigma \nabla_r^2 V$$

$$\nabla^2 V = -\rho_s \delta(z)$$

$$\rho_k \sim \exp\left(-\frac{\sigma k}{2} t\right) \rightarrow \infty$$

Instability and formation of current domains

Andreev, Aleiner, Millis, PRL 2003



Non-dissipative current domains

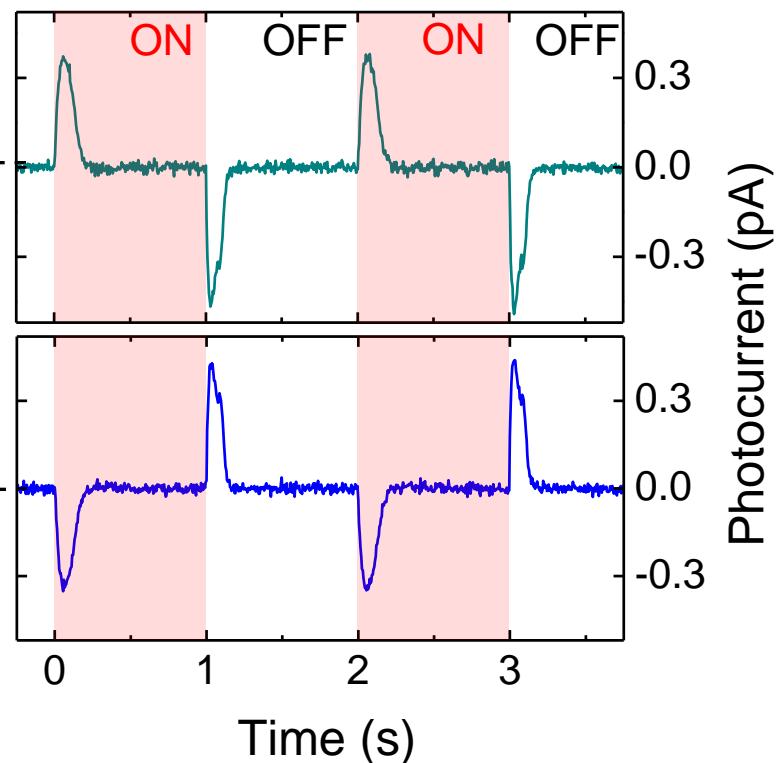
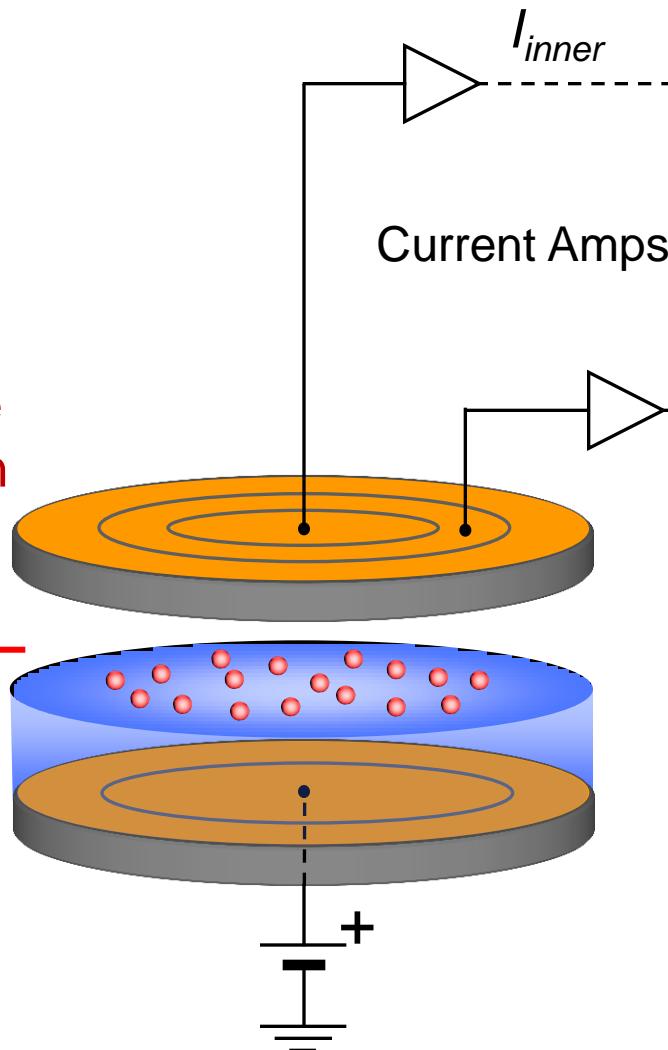
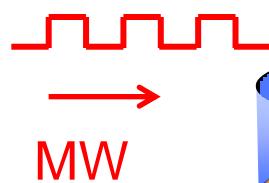
Andreev et al. PRL 2003

Photocurrent experiment

DK, Chepelianskii, Kono, J. Phys. Soc. Jpn. 2012

Fix B -field
at minima
of σ_{xx}

Microwave
modulation
ON/OFF



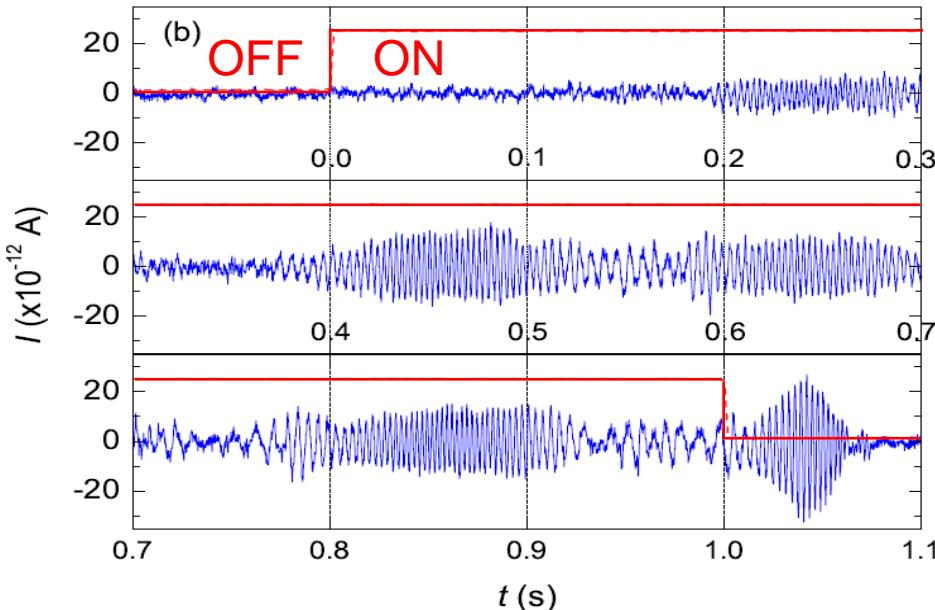
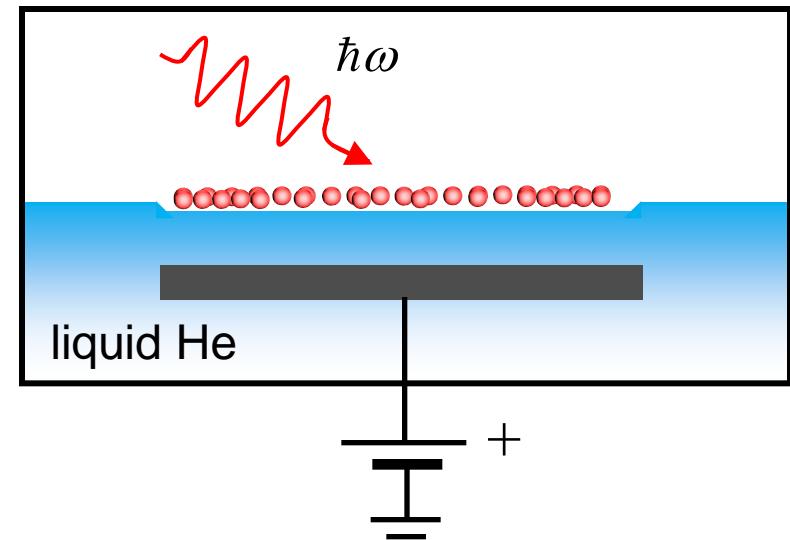
When MW switched ON
Positive image charge released
Electrons moved away

When MW switched ON

Electrons deplete from the center

AND accumulate at the edge

(large fraction up to 50%)



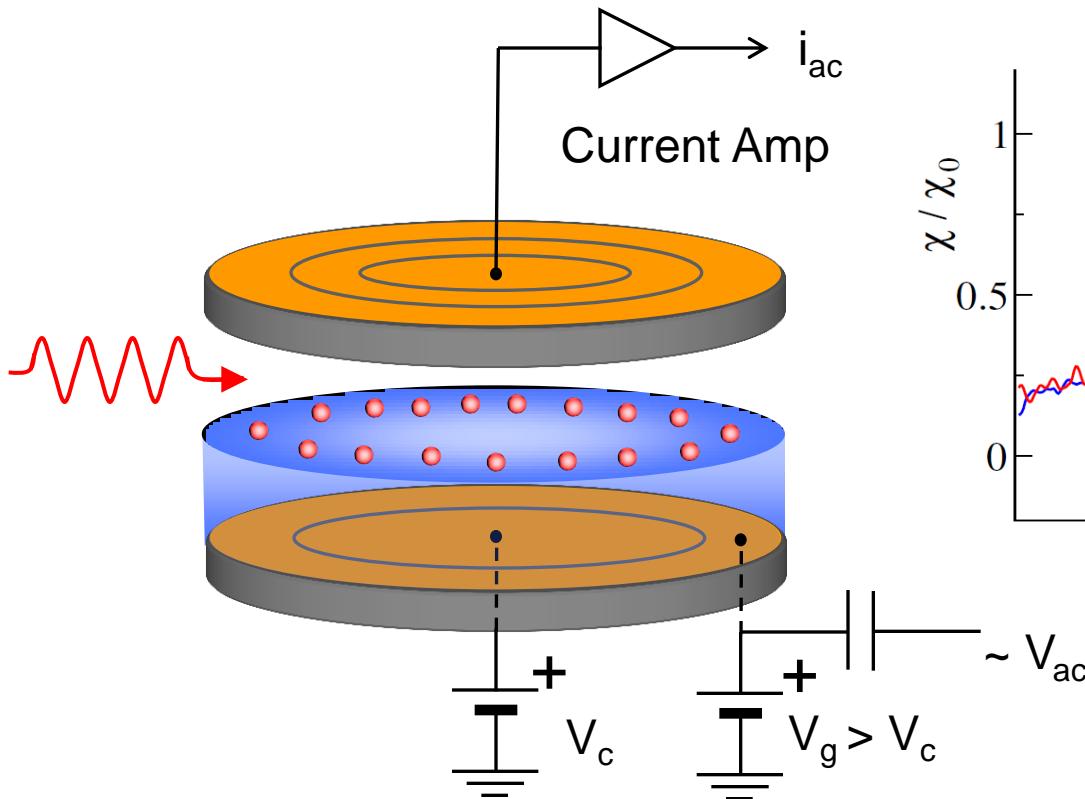
In certain range of e^- density
appears self-organized
(audio-frequency) oscillations

DK, M. Watanabe, K. Kono J. Phys. Soc. Jpn.
(2013)

Compressibility experiment

Recent experiment in RIKEN

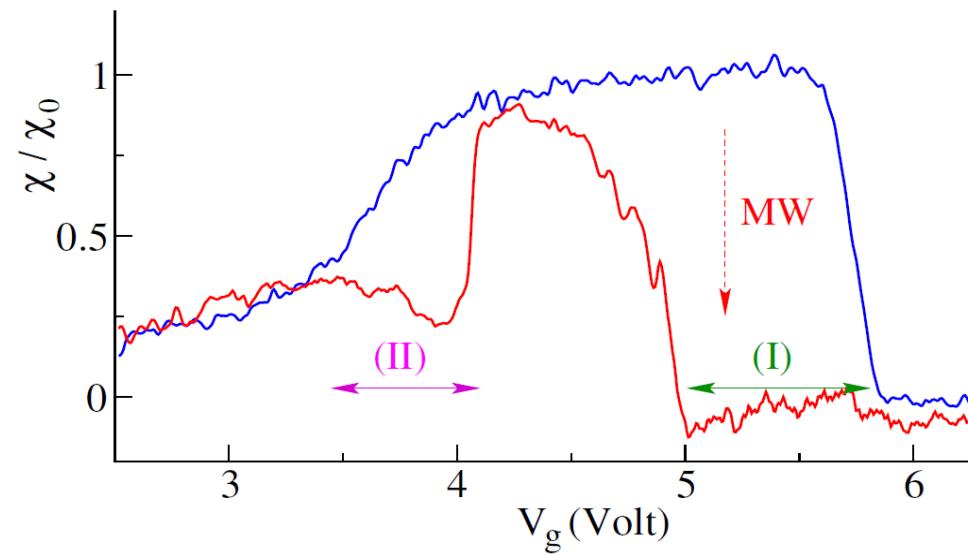
A. Chepelianskii et al. *Nature Communication*, in press



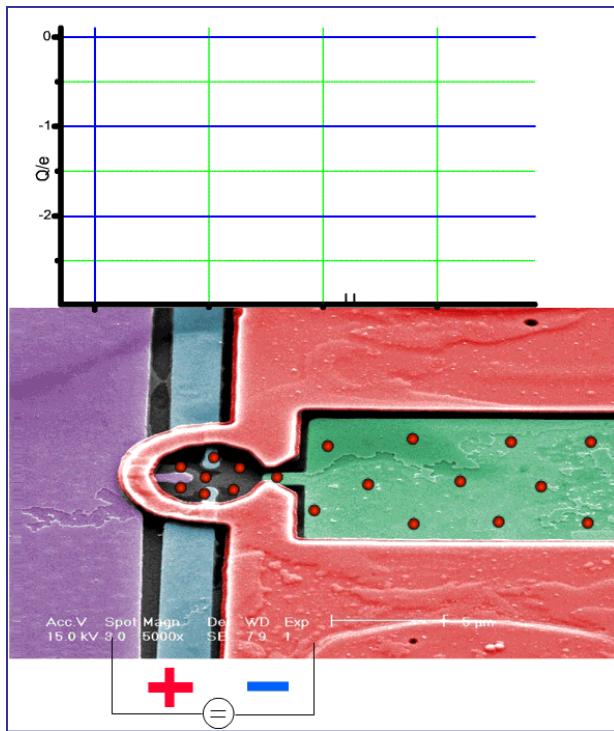
Can directly measure compressibility

defined by

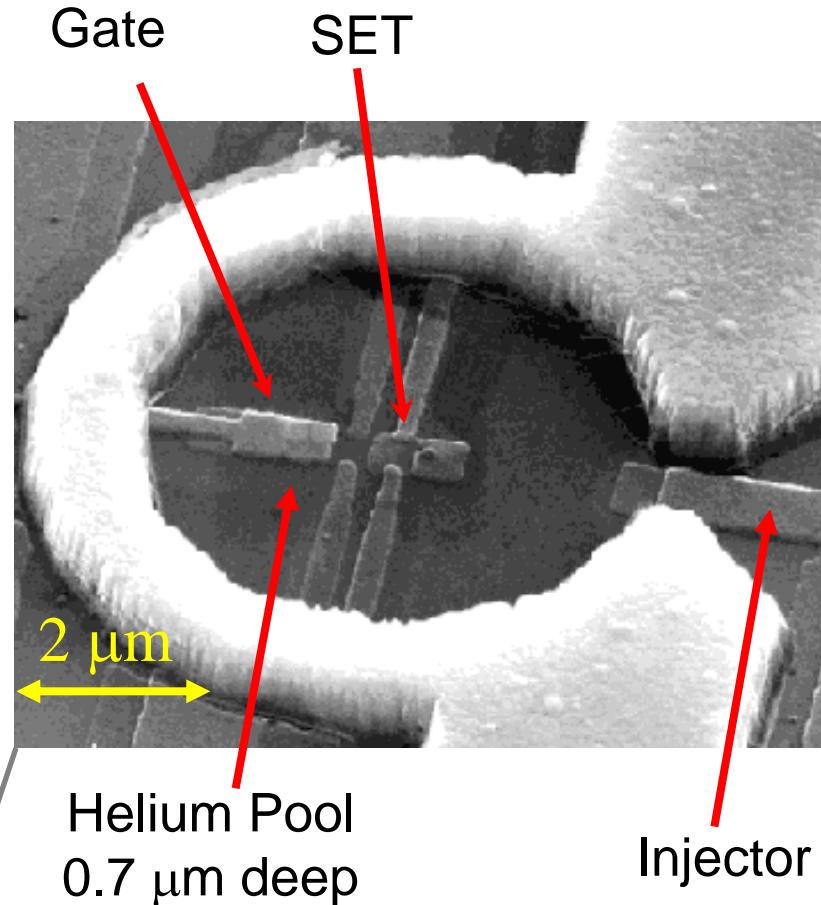
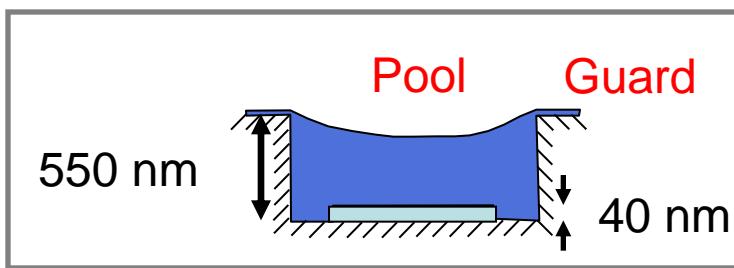
$$\chi = \frac{dn_e}{dV_g} \sim i_{ac}$$



Vanishing compressibility!



Yury Mukharsky, CEA, Saclay, France
 E. Rousseau *et al.* PRB 79, 045406(2009)



Mike Lea, RHUL, London, UK
 G. Papageorgiou *et al.* APL 86, 153106(2005)

PHYSICAL REVIEW A 74, 052338 (2006)

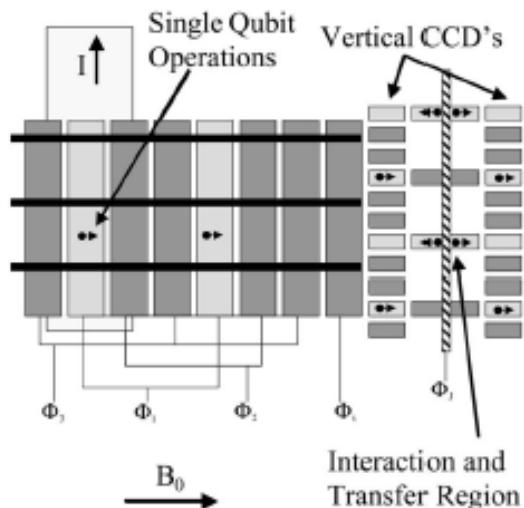
Spin-based quantum computing using electrons on liquid helium

S. A. Lyon

Department of Electrical Engineering, Princeton University, Princeton, New Jersey 08544, USA

(Received 17 September 2006; published 30 November 2006)

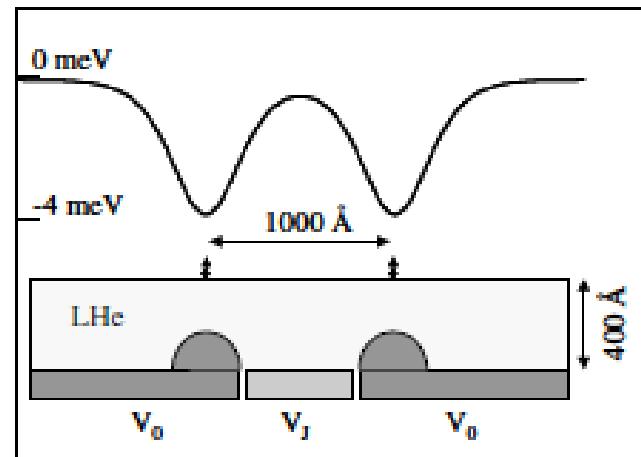
Numerous physical systems have been proposed for constructing quantum computers, but formidable obstacles stand in the way of making even modest systems with a few hundred quantum bits (qubits). Several approaches utilize the spin of an electron as the qubit. Here it is suggested that the spin of electrons floating on the surface of liquid helium will make excellent qubits. These electrons can be electrostatically held and manipulated much like electrons in semiconductor heterostructures, but being in a vacuum the spins on helium suffer much less decoherence. In particular, the spin-orbit interaction is reduced so that moving the qubits with voltages applied to gates has little effect on their coherence. Remaining sources of decoherence are considered, and it is found that coherence times for electron spins on helium can be expected to exceed 100 s. It is shown how to obtain a controlled-NOT operation between two qubits using the magnetic dipole-dipole interaction.



Fluctuating magnetic field due to Rashba effect (spin-orbit interaction):

$$H_{s-o} = \alpha(\mathbf{p}_\parallel \times \mathbf{E}_\perp) \cdot \hat{S}$$

- T_2 exceeding 100 sec
- Qubit coupling by dipole interaction



[S. A. Lyon, Phys. Rev. A, 74, 052338]

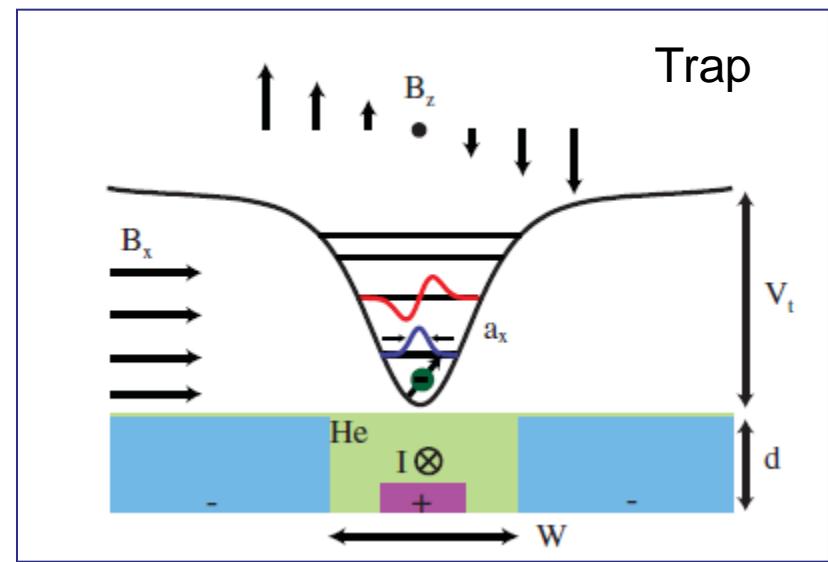
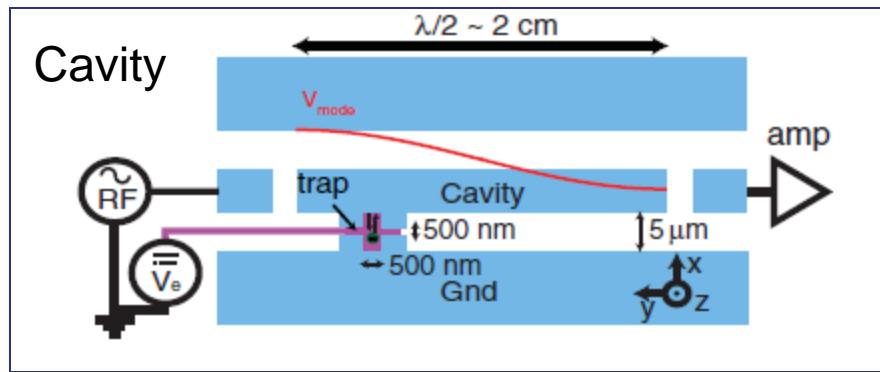
Proposal for Manipulating and Detecting Spin and Orbital States of Trapped Electrons on Helium Using Cavity Quantum Electrodynamics

D. I. Schuster,¹ A. Fragner,¹ M. I. Dykman,² S. A. Lyon,³ and R. J. Schoelkopf¹

¹*Department of Applied Physics and Physics, Yale University, New Haven, Connecticut 06511, USA*

²*Department of Physics and Astronomy, Michigan State University, East Lansing, Michigan 48824-2320, USA*

³*Department of Electrical Engineering, Princeton University, Princeton, New Jersey 08544, USA*



- Strong coupling to RF cavity
- Electron-electron coupling via a single photon
- Manipulation of spin states via spin-orbit coupling

Progress: APS March Meeting 2012

- Electrons on helium: unique model system
- New quantum phenomena under MW excitation
- Some remarkable progress in quantum engineering
 - Steve Lyon, Princeton: CCD device
 - Mike Lee, University of London Royal Holloway and
 - Yuriy Moukharskii, Sacley: SET
 - David Rees, NCTU-RIKEN Joint Laboratory: Point Contact
 - David Shuster, University of Chicago and
 - Andreas Fragner, Yell University: Cavity QED
- end more..
- Still exciting object of study!